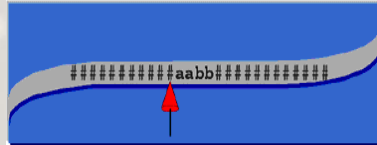


quantum machines... for computing

Alan Turing



the universal Turing machine



Church-Turing thesis

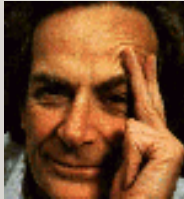
sequential computing

quantum aspects relevant?

John von Neumann



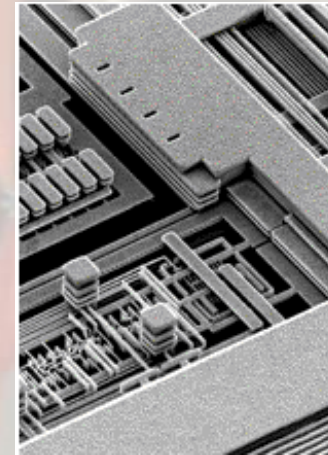
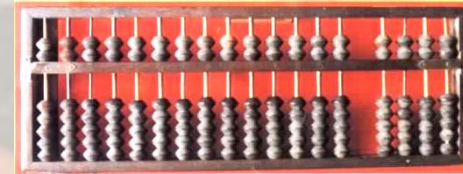
Richard Feynman



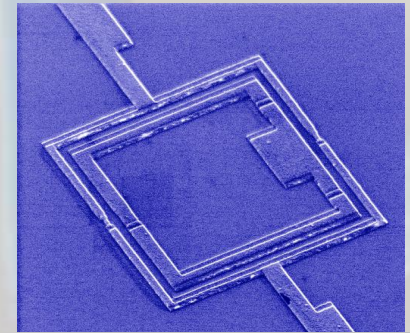
David Deutsch



Richard Jozsa

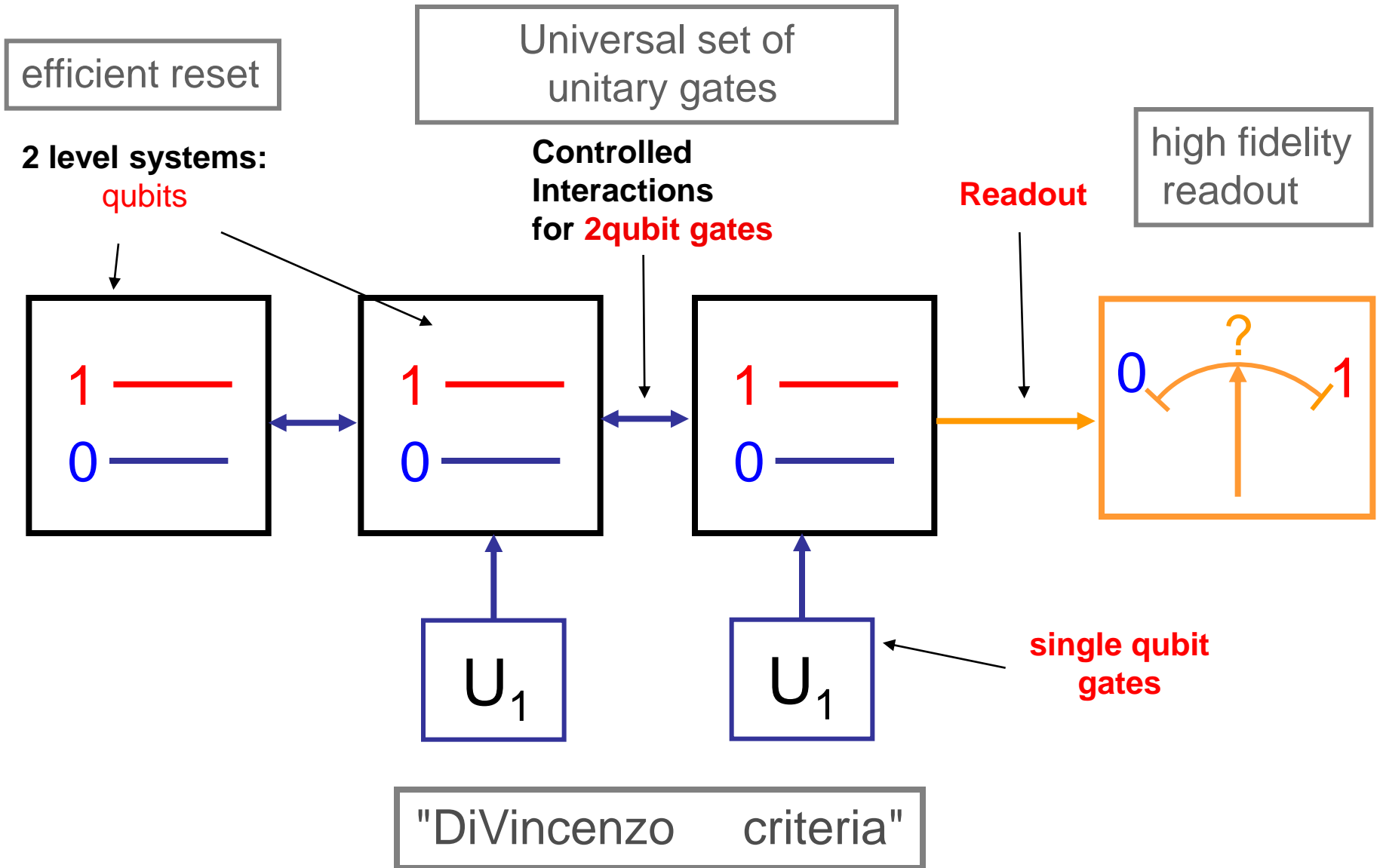


1982:
algorithmic complexity
is not only maths !



quantum computing
more powerful than sequential computing

Schematic blueprint of a quantum processor



Ideal qubit readout :

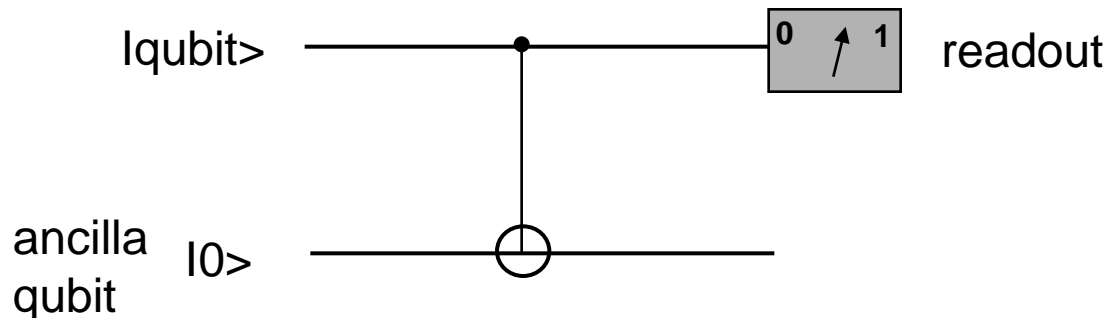
Projective measurement of $|\Psi\rangle = \alpha|0_1\rangle \otimes |\Psi_{2\dots N}\rangle + \beta|1_1\rangle \otimes |\Psi'_{2\dots N}\rangle$

yields $\left\{ \begin{array}{l} \text{readout 0 and state } |0_1\rangle \otimes |\Psi_{2\dots N}\rangle \text{ with prob } |\alpha|^2 \\ \text{or} \\ \text{readout 1 and state } |1_1\rangle \otimes |\Psi'_{2\dots N}\rangle \text{ with prob } |\beta|^2 \end{array} \right.$

Readout fidelity (for answer)

if non destructive: **Projection fidelity** for state after readout (QND ?)

Note: A high fidelity destructive readout can be made QND :



Lecture fidèle non-destructive d'un qubit supraconducteur

QUANTRONICS GROUP
(SPEC, CEA-Saclay branch)

F. Mallet, F. Ong, A. Palacios-Laloy, F. Nguyen,
P. Sénat, P. Orfila P. Bertet, D. Vion, D. Estève
with the help of Quantronics

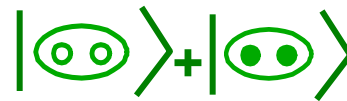
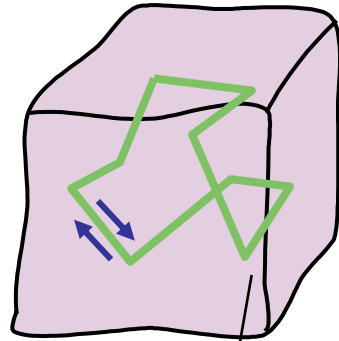
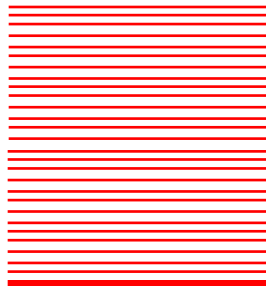


Superconductivity helps making qubits

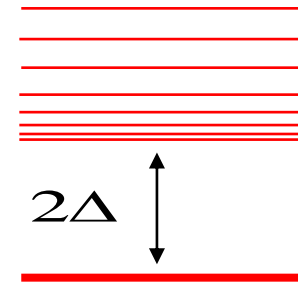
Energy spectrum of an isolated electrode

Non superconducting state

N



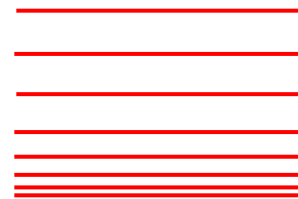
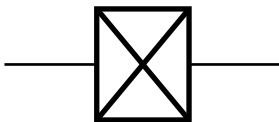
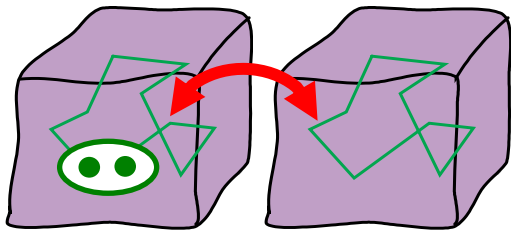
Superconducting state



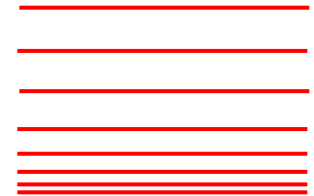
S

singlet ground state

The Josephson junction



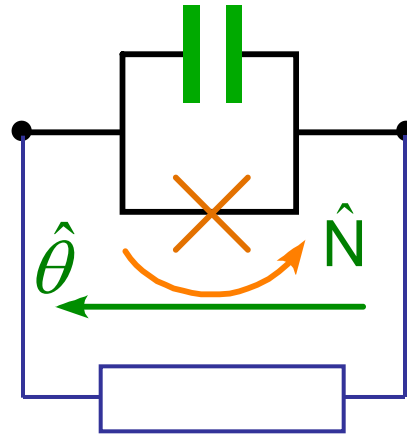
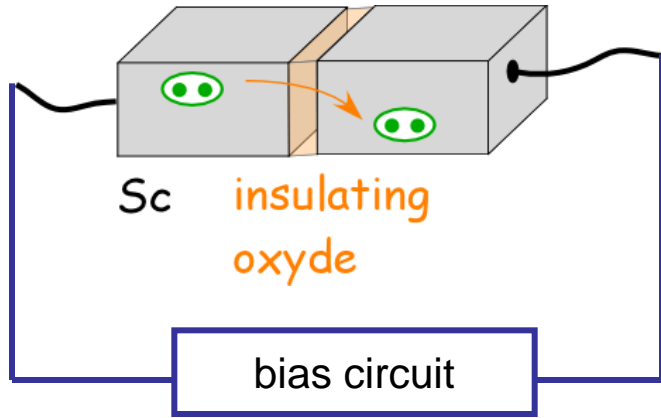
2Δ



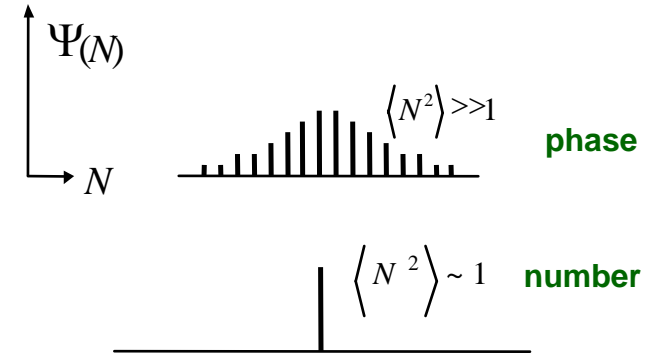
2Δ



The single Josephson junction circuit



θ and N conjugated variables

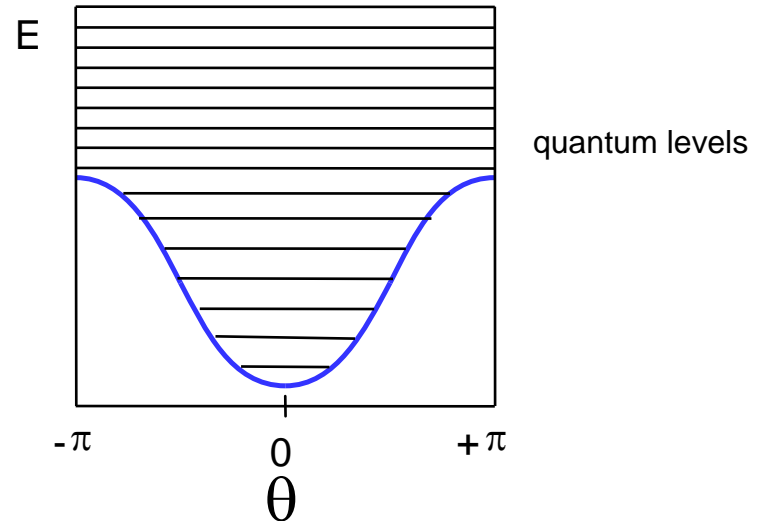


Hamiltonian:

$$H = H_J + H_{elm}$$

Josephson Hamiltonian:

$$H_J = -E_J \cos \hat{\theta}$$

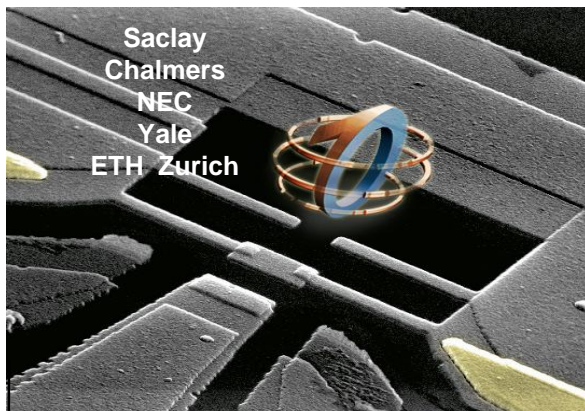


superconducting qubits come in different flavors

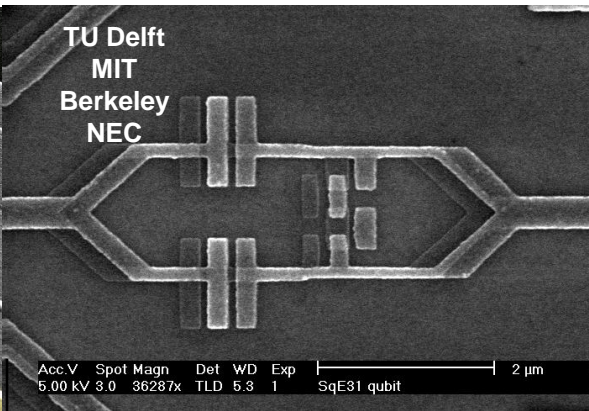
Various types of superconducting qubits

Cooper-pair boxes

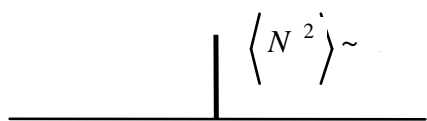
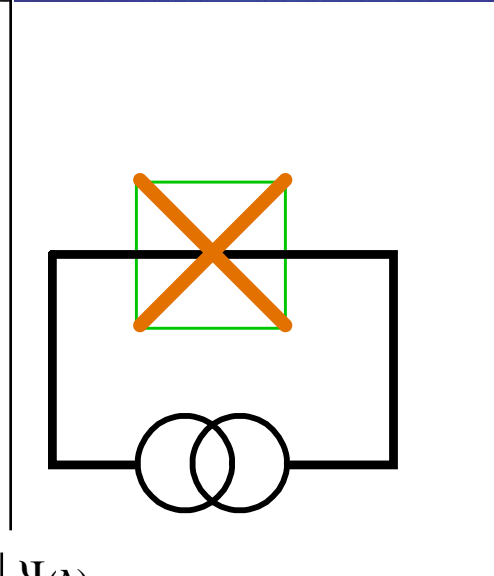
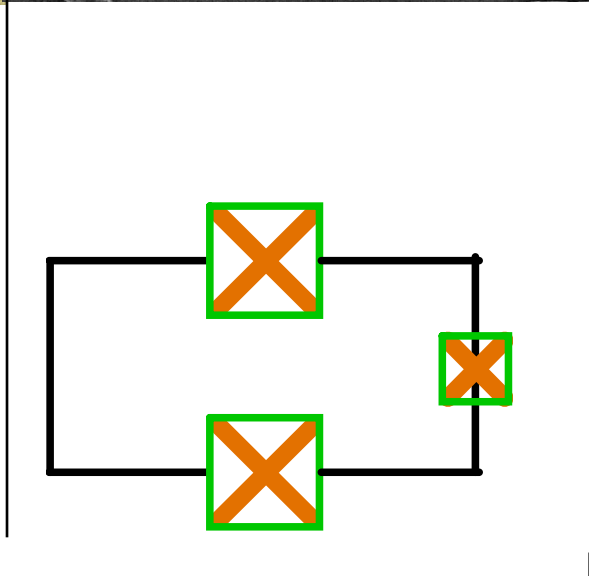
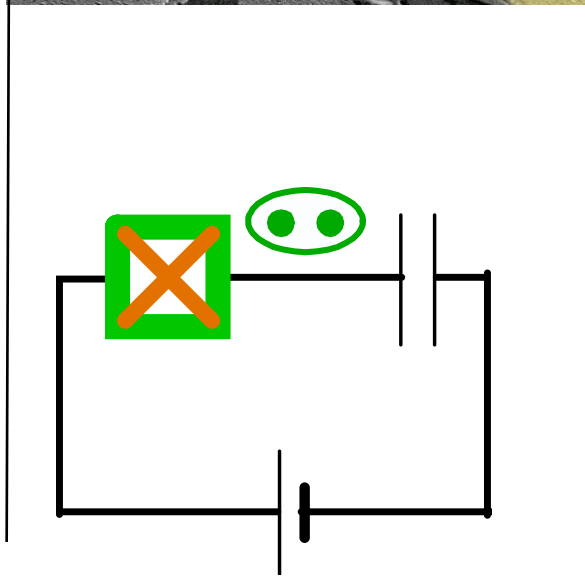
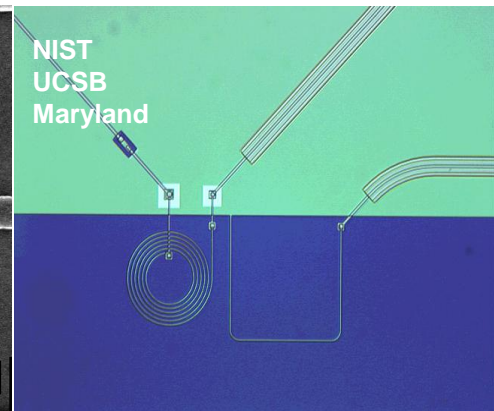
Charge qubit/Quantronium/Transmon



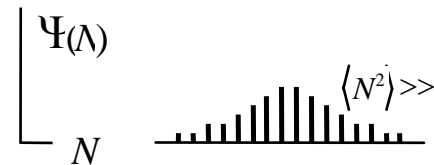
Flux qubits



Phase qubits



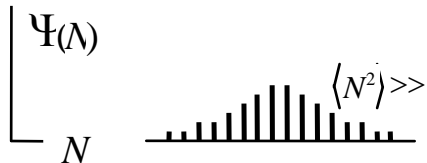
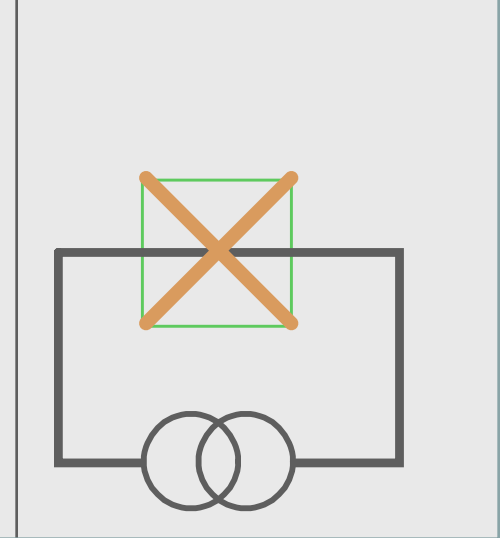
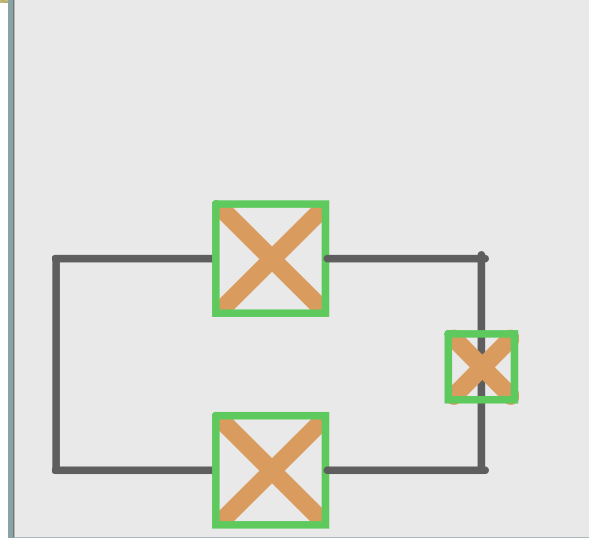
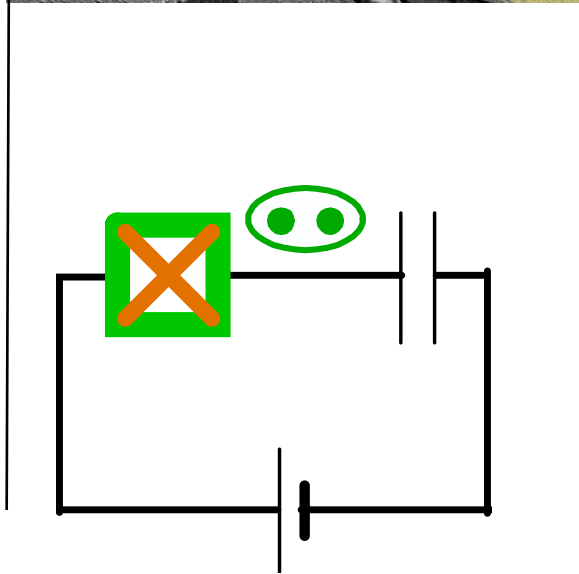
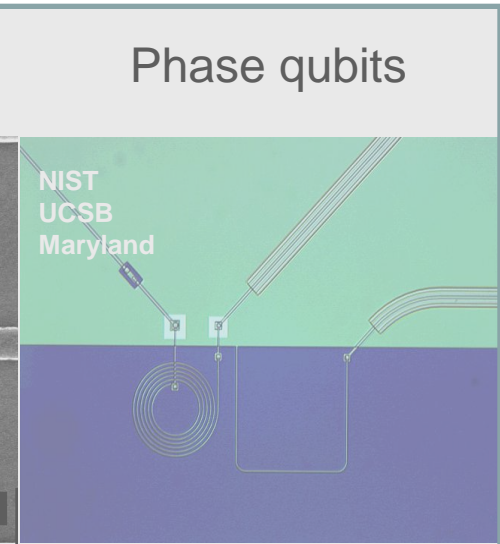
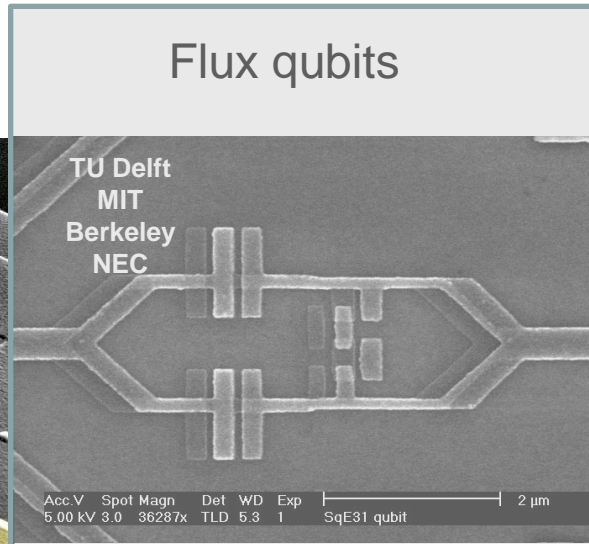
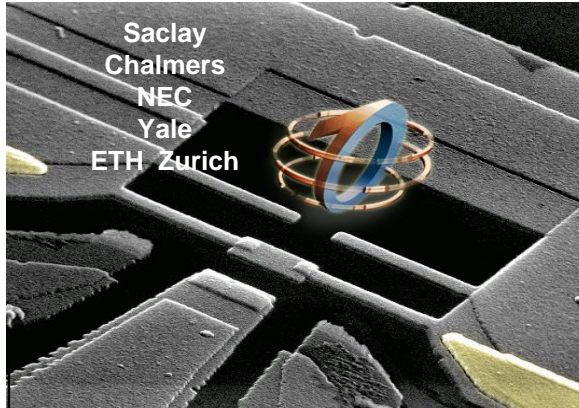
naively: from number to phase states



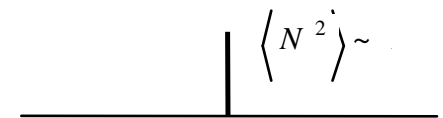
Various types of superconducting qubits

Cooper-pair boxes

Charge qubit/Quantronium/**Transmon**

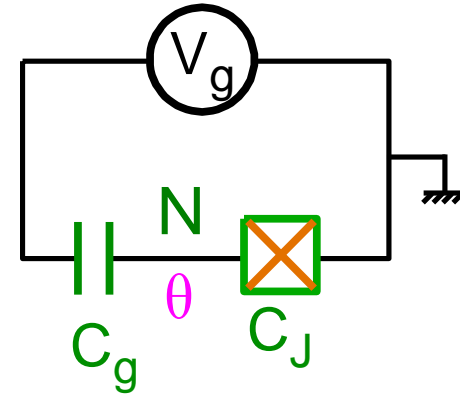
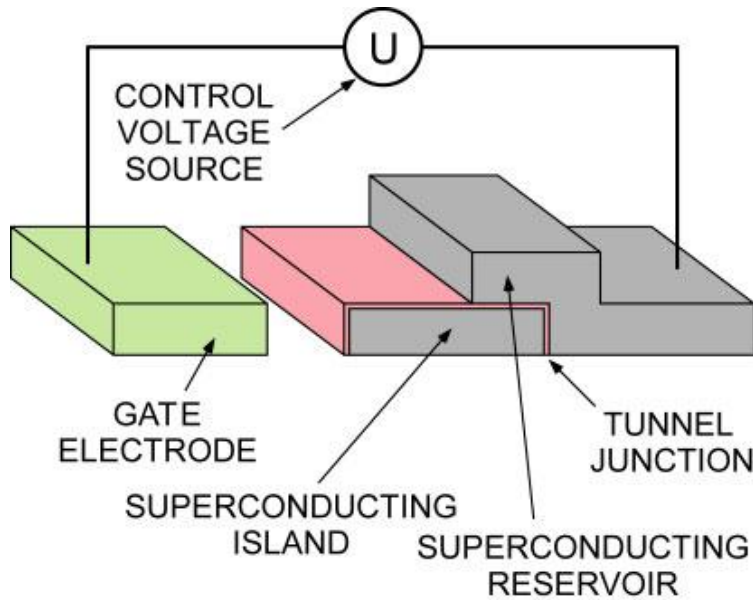


← CPBs cover the whole range →



simplest superconducting artificial atom: the Cooper pair box

Quantronics 1996
NEC1999



1 degree of freedom: $[\hat{\theta}, \hat{N}] = i$

1 knob: V_g or $N_g = C_g V_g / (2e)$

2 characteristic energies: $E_J = \frac{h\Delta}{8e^2 R_t}$

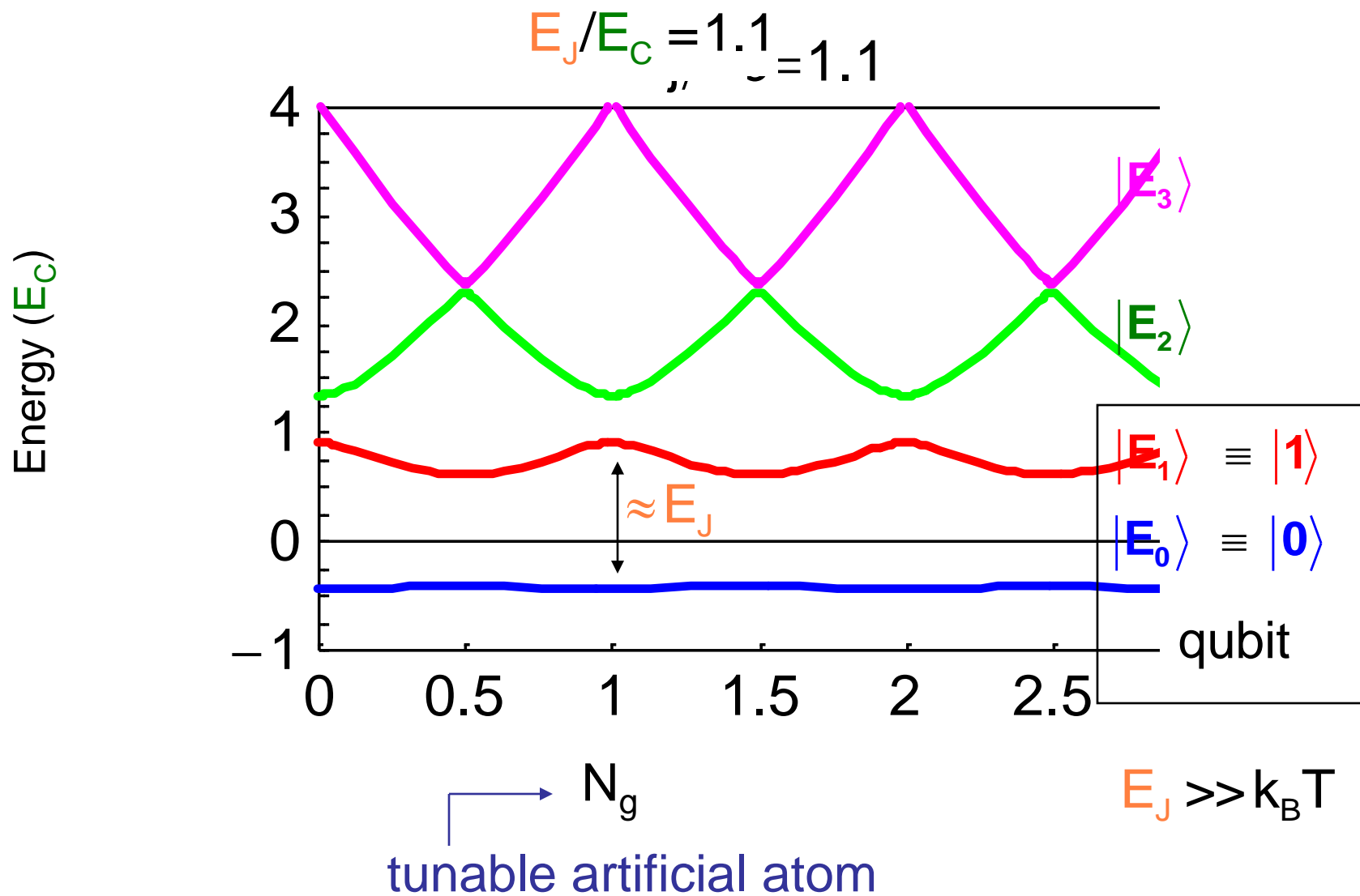
$$E_C = \frac{(2e)^2}{2(C_g + C_J)}$$

Hamiltonian: $\hat{H} = E_C (\hat{N} - N_g)^2 - E_J \cos \hat{\theta}$

↑
Electrostatic

↑
Phase difference cost

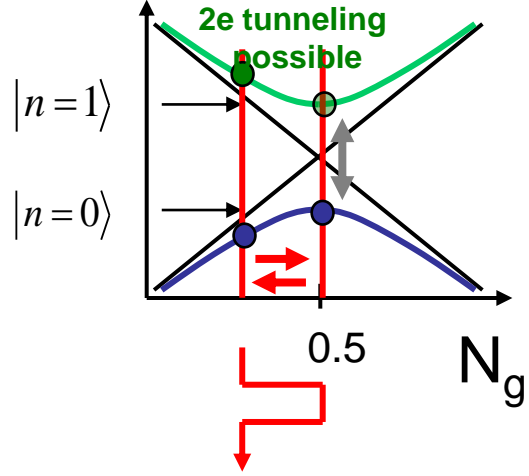
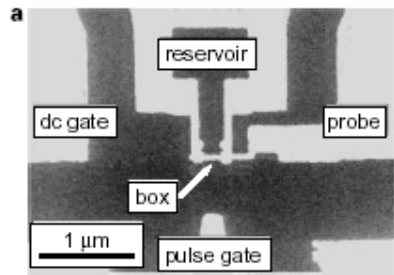
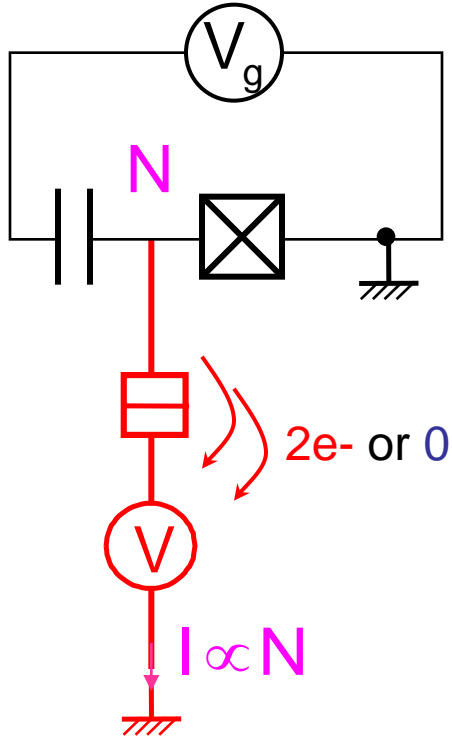
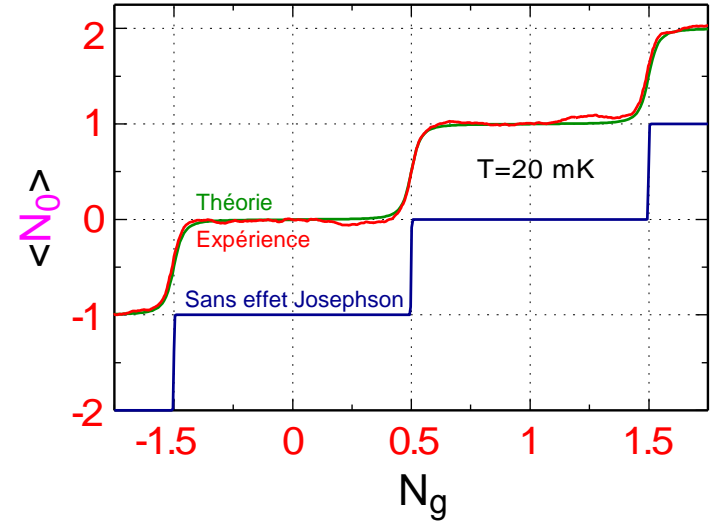
Hamiltonian and energy spectrum



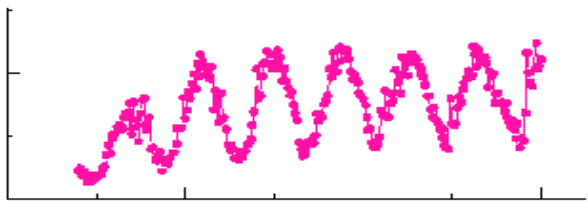
Cooper Pair box coherence : ten years after (I)

Prehistory: ground state charge
(Quantronics 1996)

Quantum coherence
(NEC, 1999)



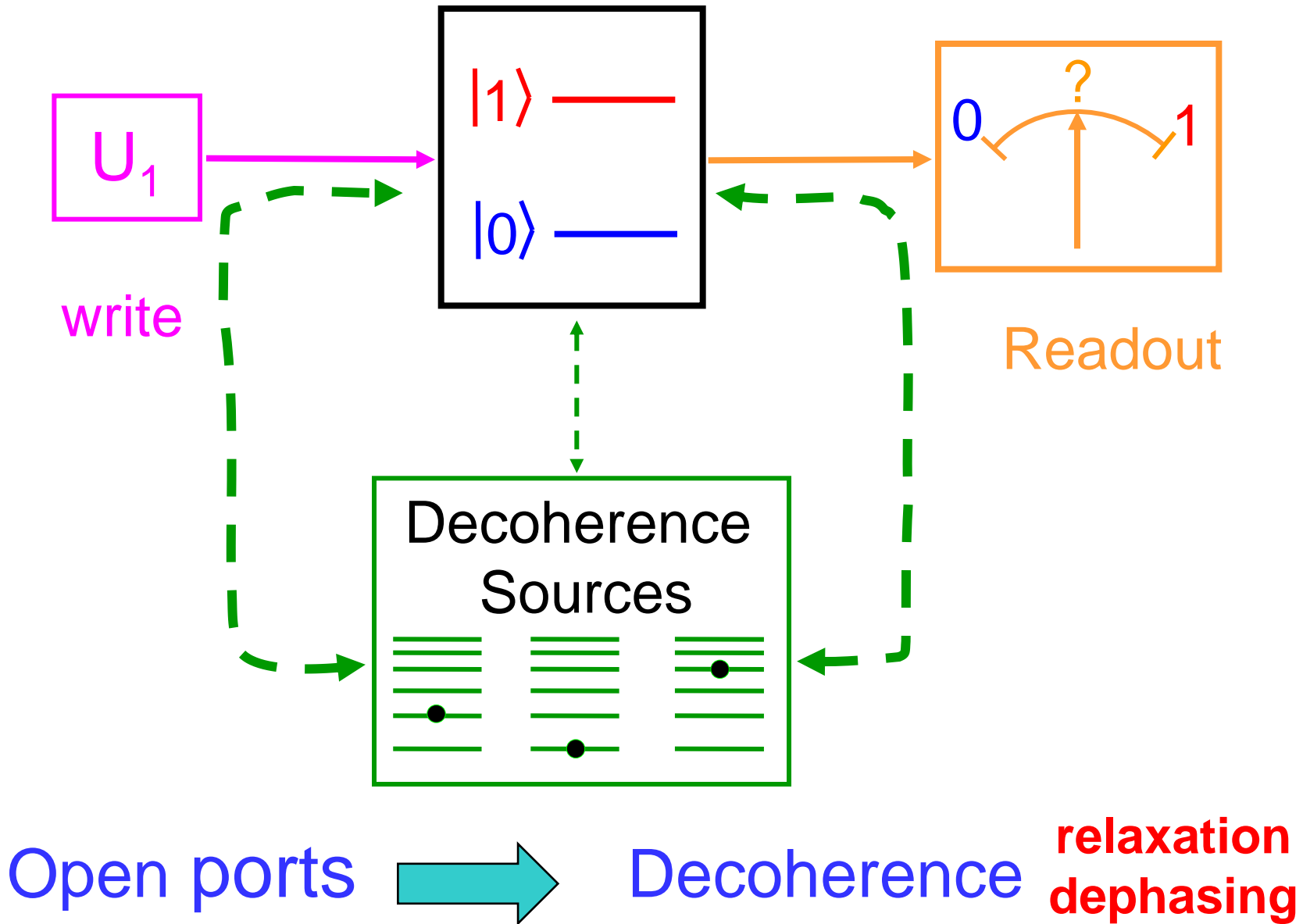
Rabi Oscillations signal



Coherence time:
5-10 ns

Pulse duration Δt (ps)

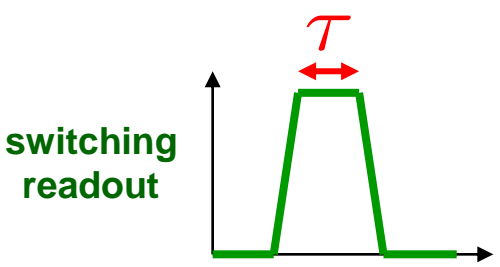
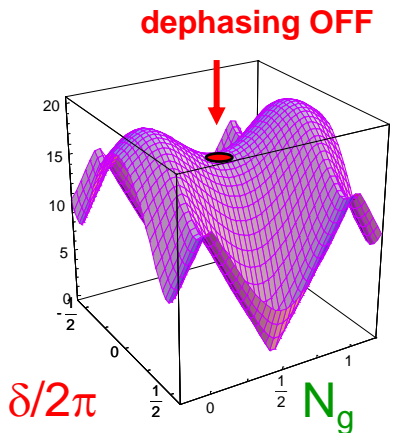
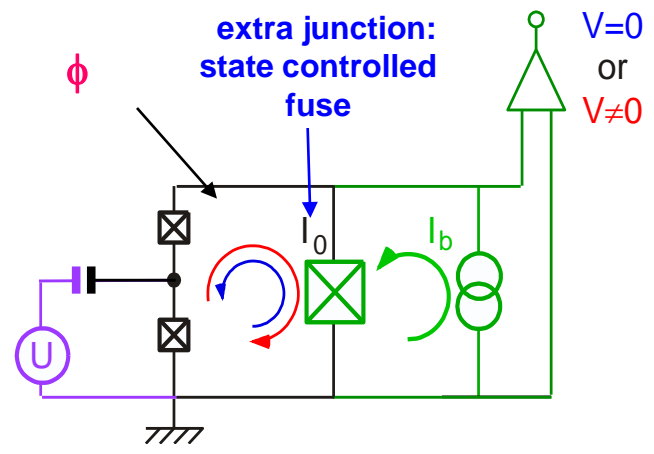
The main (?) difficulty



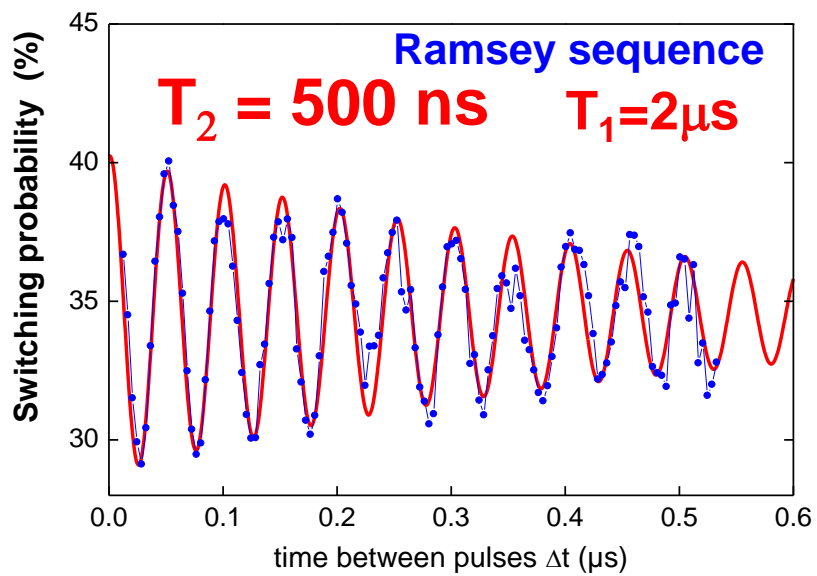
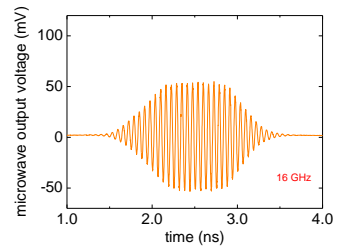
Cooper Pair box coherence : ten years after (II)

a CPB with single shot readout and a strategy against dephasing: **the quantronium** (Quantronics 2001)

Vion et al., Science 296 (2002)



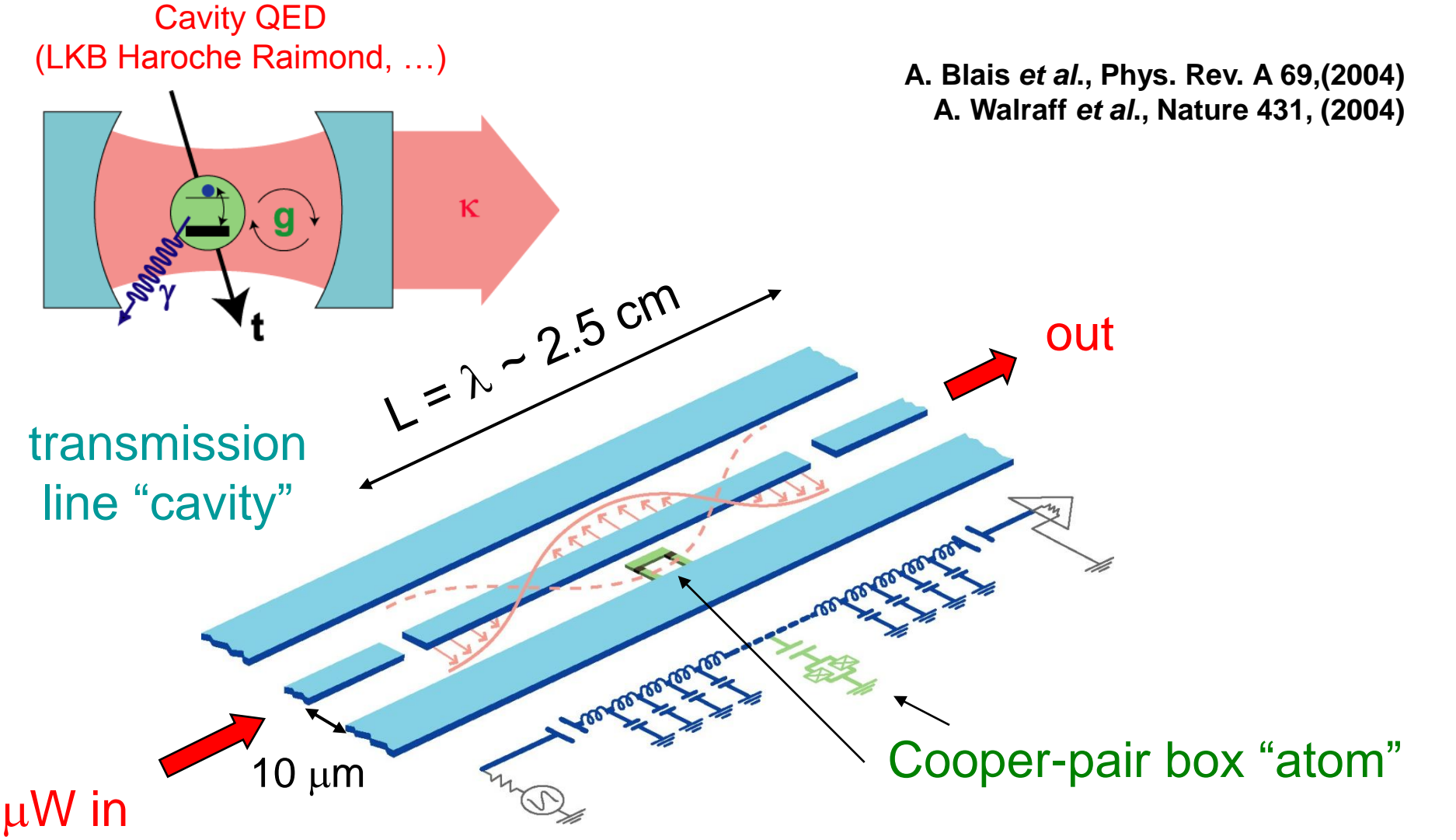
Resonant drive



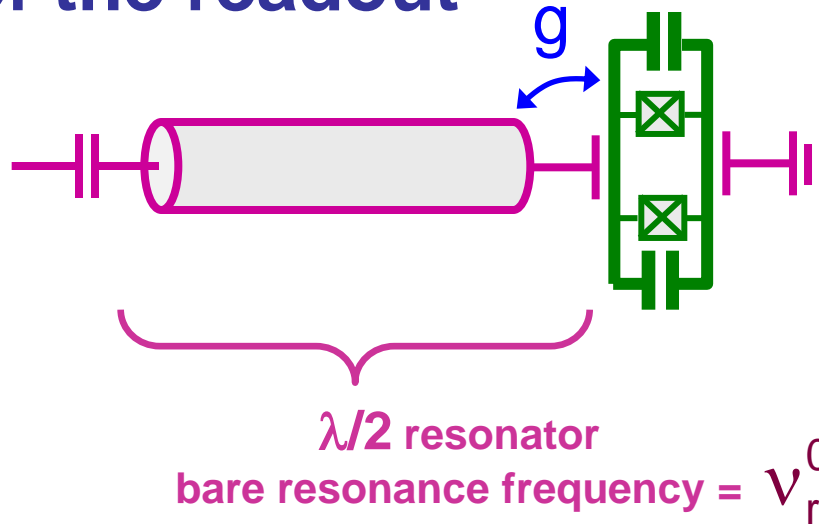
x100 gain
Coherence and readout fidelity still limited
more complex circuits do not work well

Cooper Pair box coherence : ten years after (III)

A CPBox embedded in a 1D microwave cavity (Yale 2003)

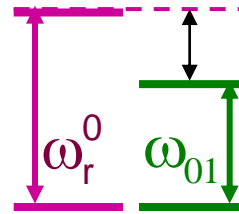


Principle of the readout



Dispersive regime

$$|\Delta| = |\omega_{01} - \omega_r^0| \gg g$$

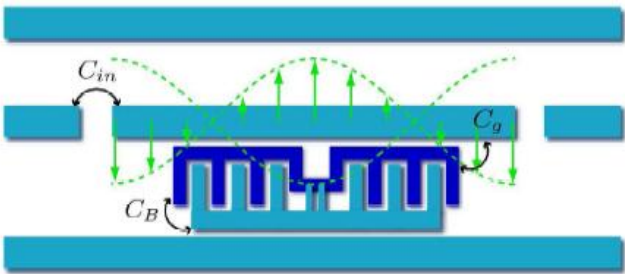


$$\hat{H}_{\text{eff}} = -\frac{\hbar}{2}(\omega_{01} + \chi)\hat{\sigma}_z + \hbar(\omega_r^0 - \chi\hat{\sigma}_z)\hat{a}^+\hat{a}$$

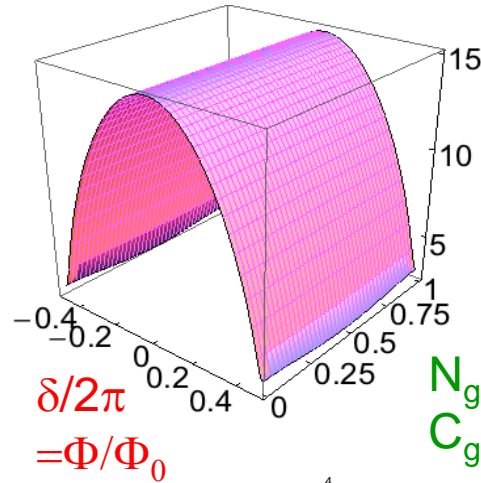
Qubit controlled Cavity pull

Cooper Pair box coherence : ten years after (III)

A CP Box $E_J \gg E_C$ insensitive to charge noise: **the transmon** (Yale 2007)



added interdigitated C

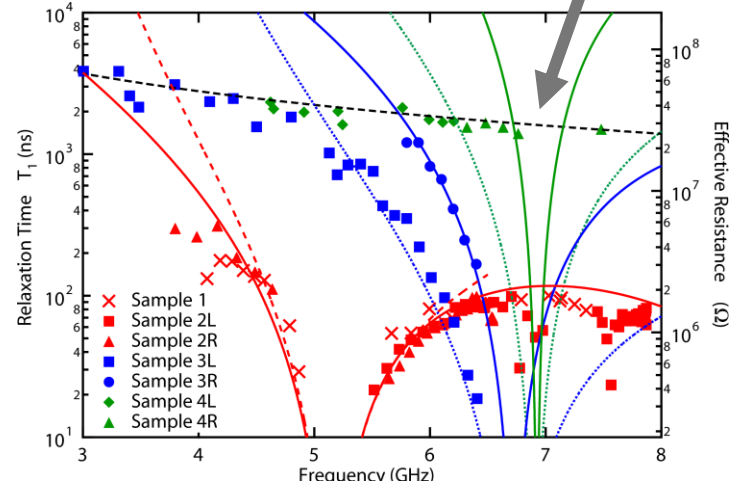
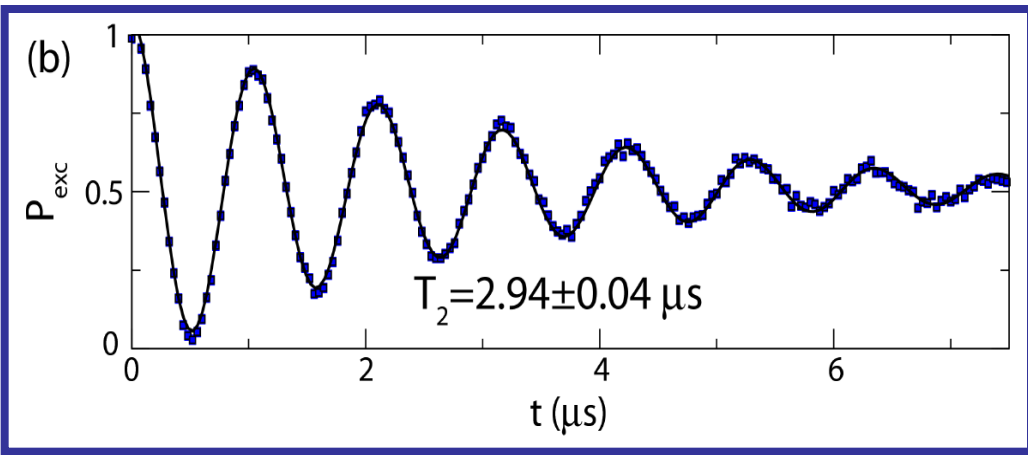


Koch et al., PRA 76 (2007)
Schreier et al., PR B 77, (2008)

flat CPB bands

$$N_g = C_g V_g / 2e$$

saturation origin ?



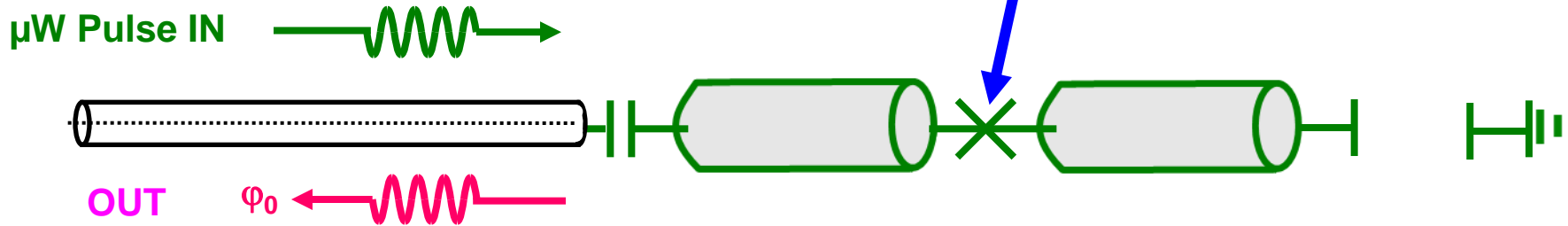
progress on coherence, **but**
high fidelity readout still missing !

'our' Solution: the Josephson Bifurcation Amplifier (JBA)

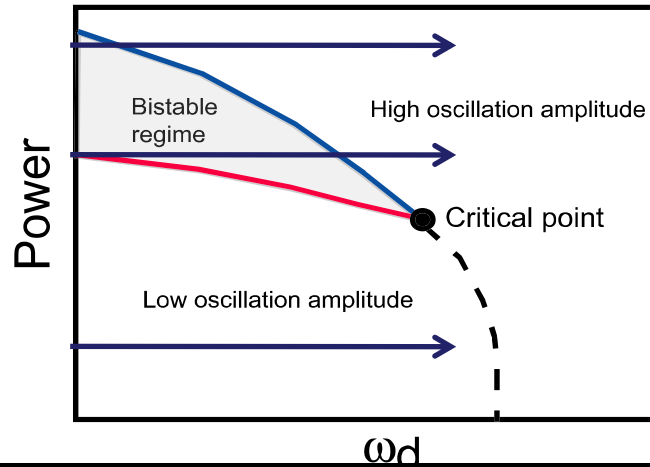
M. Devoret Qulab (Yale)

JBA: I. Siddiqi et al., PRL 93 (2004)

cavity JBA: M. Metcalfe et al. PRB 76 (2007)



Dynamical bifurcation transition
to high oscillation amplitude
in a non-linear oscillator



Readout: the bifurcation transition threshold depends on qubit state

Note: other transitions possible: i.e. onset of parametric oscillations , ...

Josephson Bifurcation Amplifier realizations:

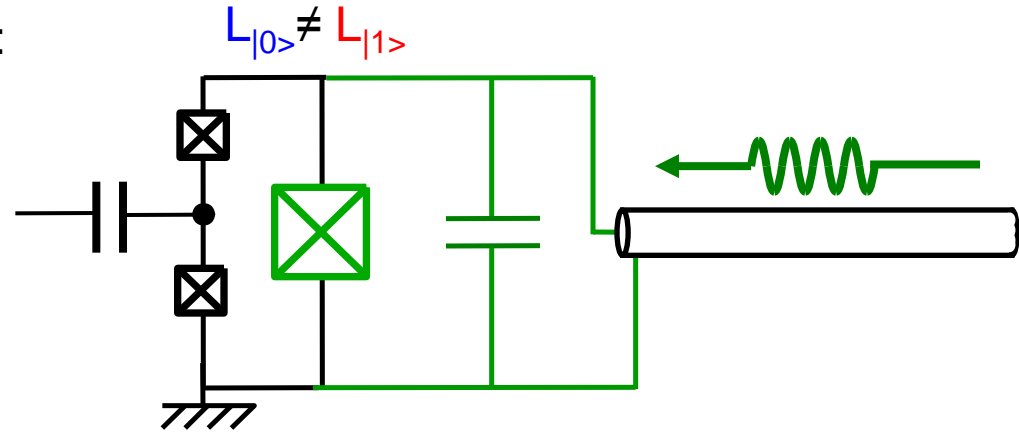
lumped element version on Quantronium:

Qulab, Yale

contrast=48%
 $T_2 \sim 300\text{ns}$ ($\neq 2T_1$)

Quantronics

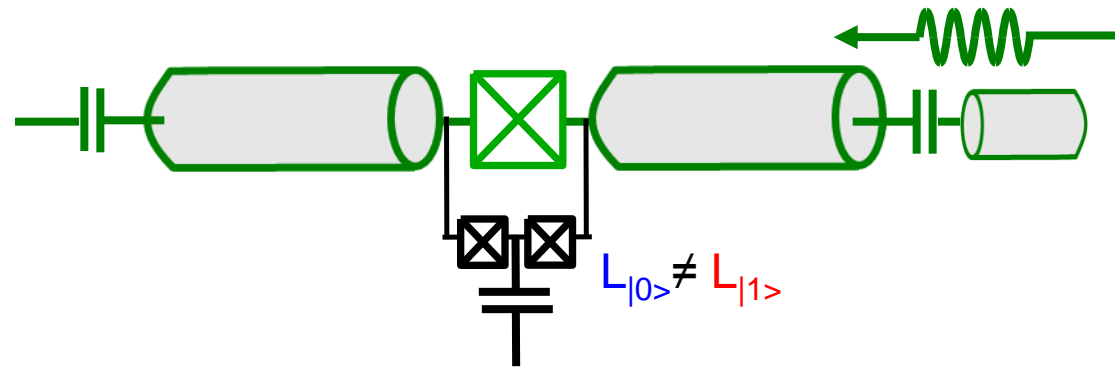
contrast=51%
 $T_2 \sim 120\text{ns}$ ($\neq 2T_1$)



distributed version on Quantronium:

Qulab, Yale

contrast=60%
 $T_2 \sim 500\text{ns}$ ($\neq 2T_1$)



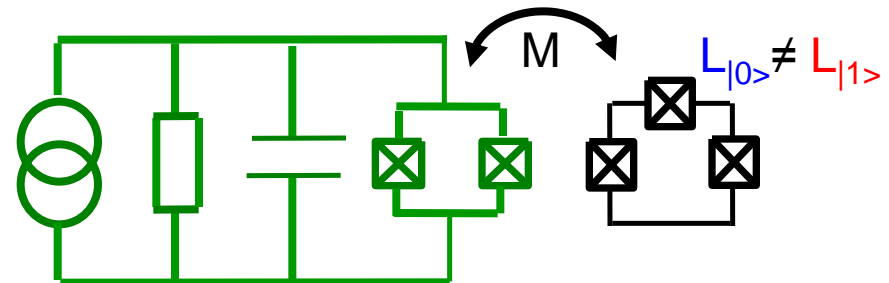
lumped version on flux qubit:

J.E. Mooij Group, T U Delft

contrast=87%
 $T_2 \sim 100\text{ns}$ ($\neq 2T_1$)

Lupascu et al.,
Nature Physics 3
(2007)

QND

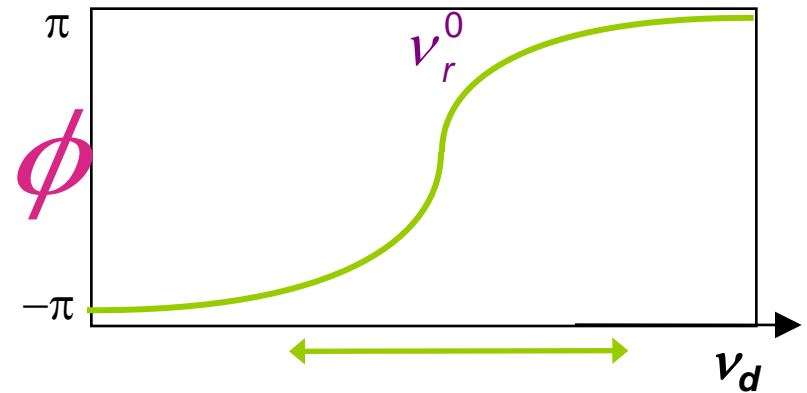
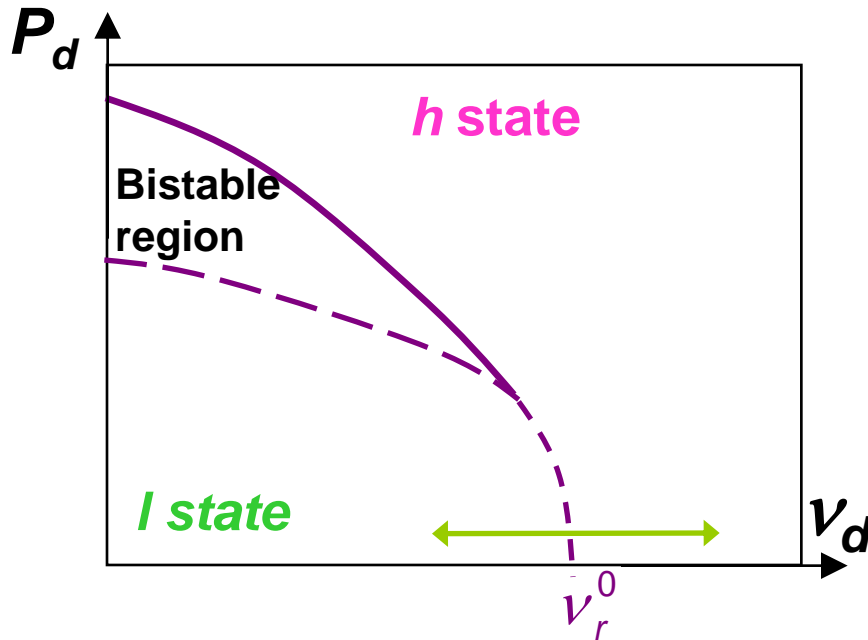
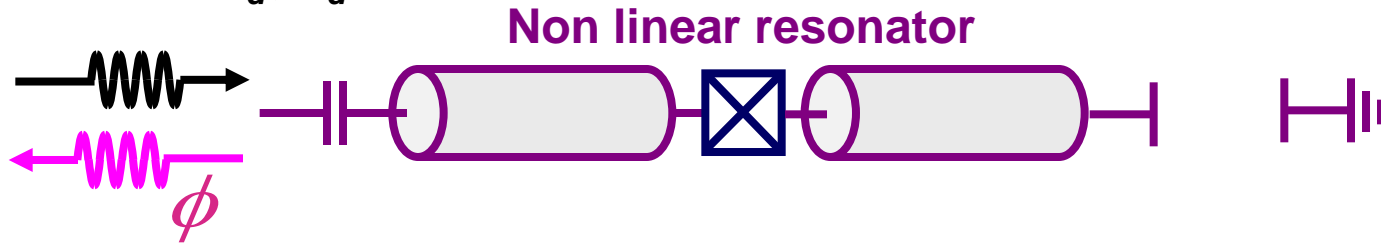


The Cavity Josephson Bifurcation Amplifier

JBA: I. Siddiqi et al., PRL 93, 207002 (2004)

CJBA: M. Metcalfe et al., Phys. Rev. B 76, 174516 (2007)

MW drive : P_d, v_d

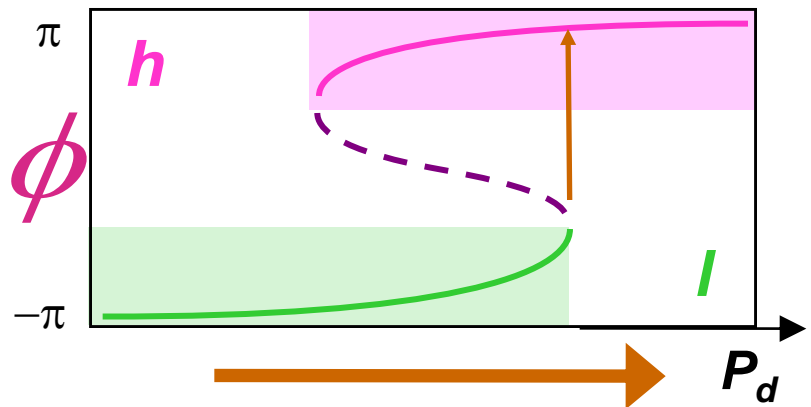
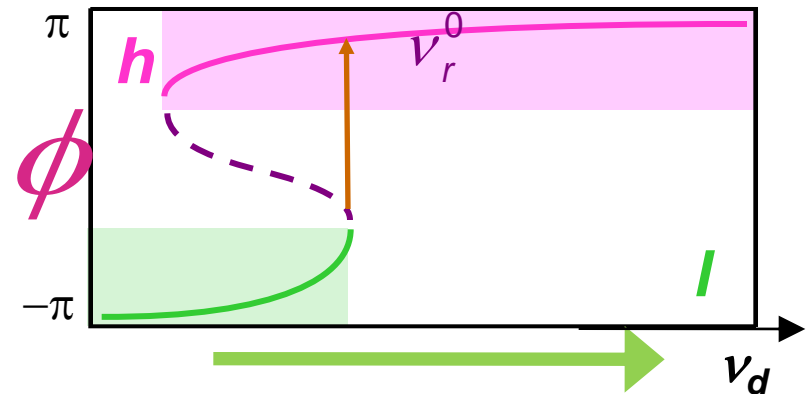
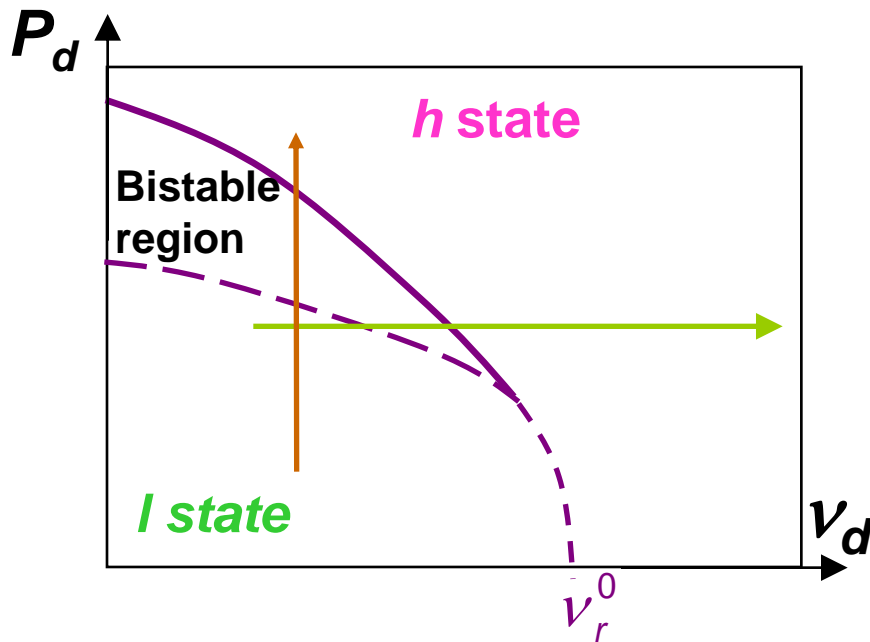
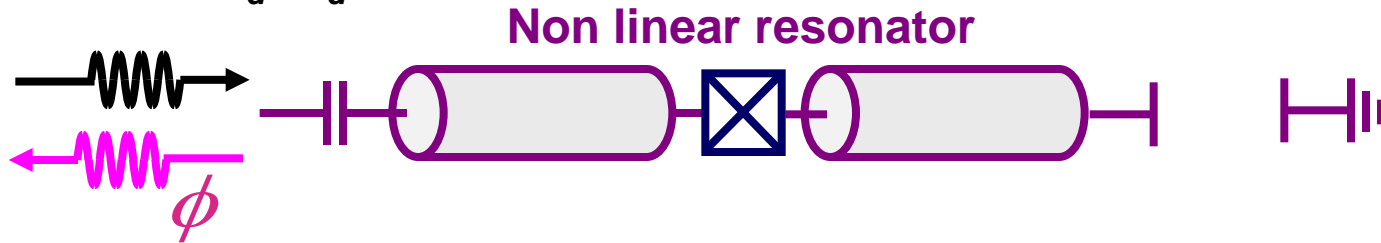


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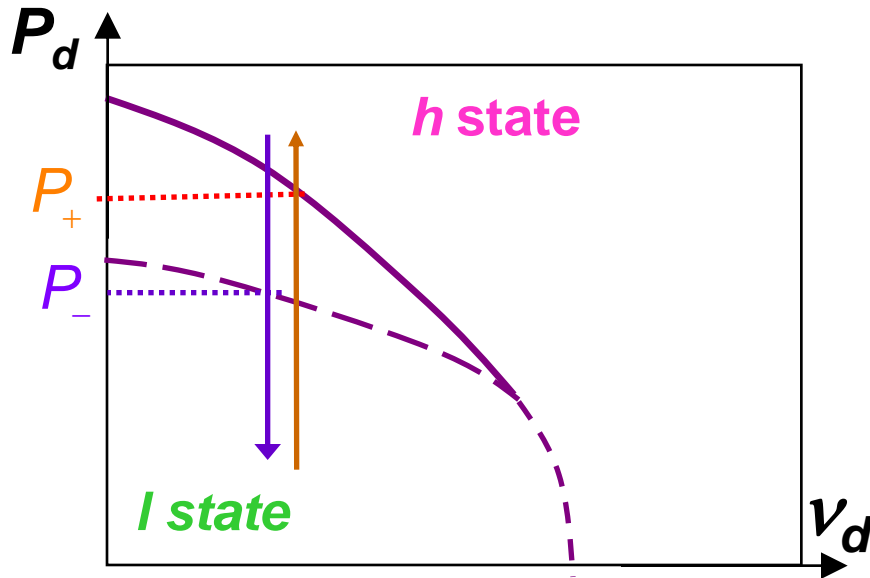
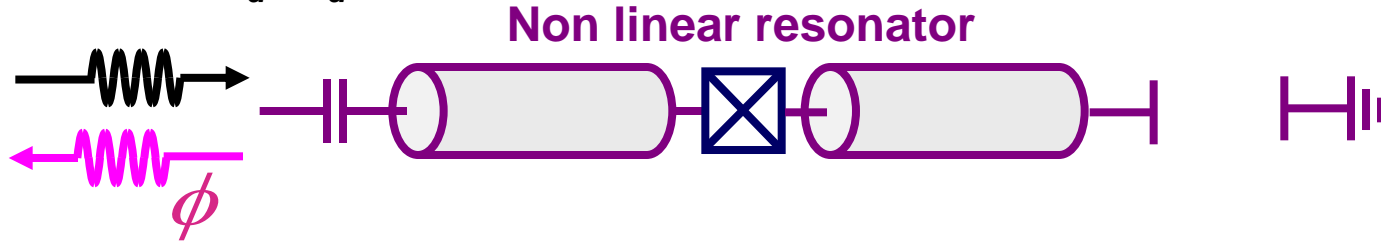


The Cavity Josephson Bifurcation Amplifier

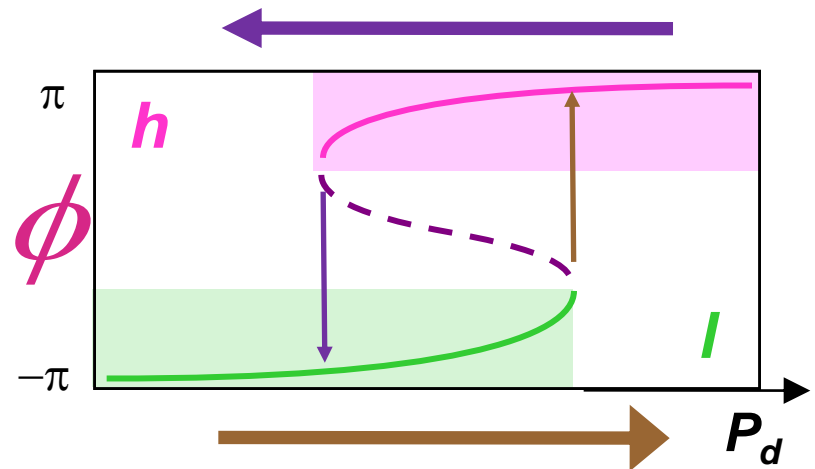
JBA: I. Siddiqi et al., PRL 93, 207002 (2004)

CJBA: M. Metcalfe et al., Phys. Rev. B 76, 174516 (2007)

MW drive : P_d, v_d

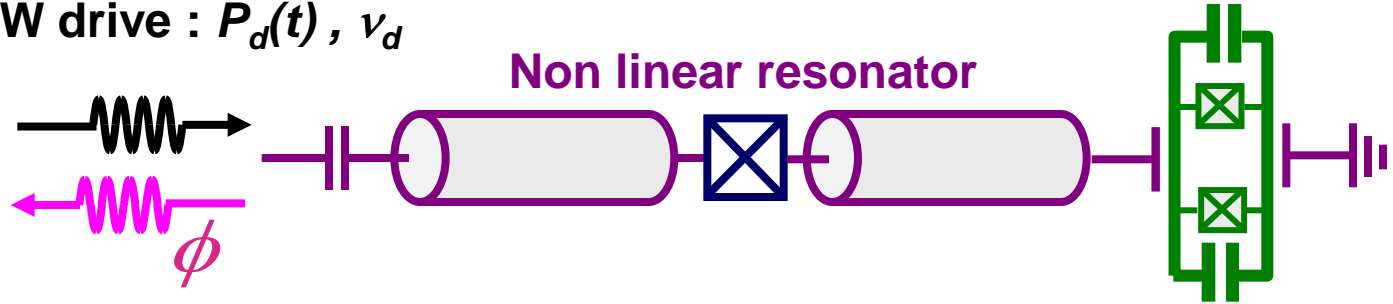


Large drive power :
BIFURCATION + HYSTERESIS

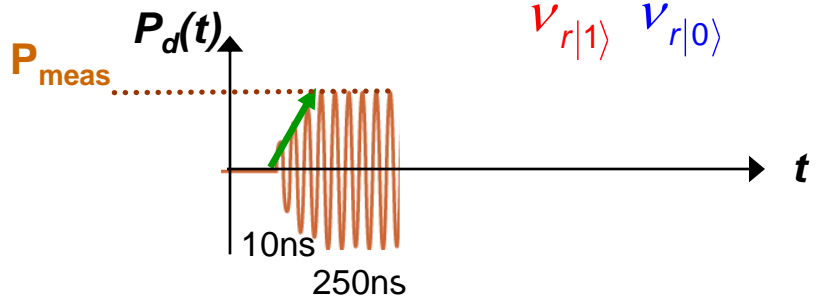
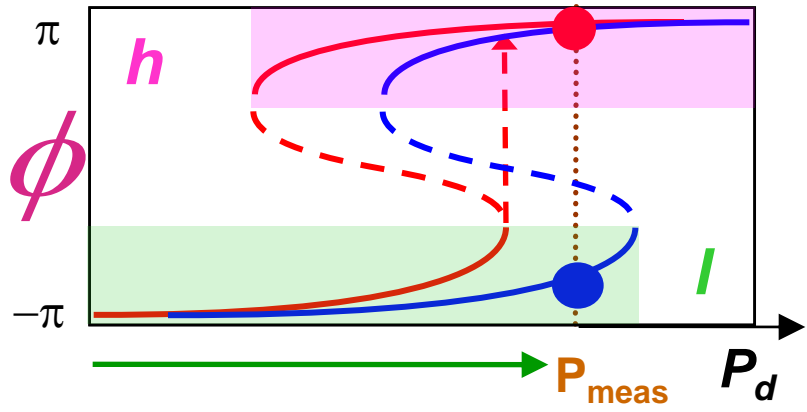
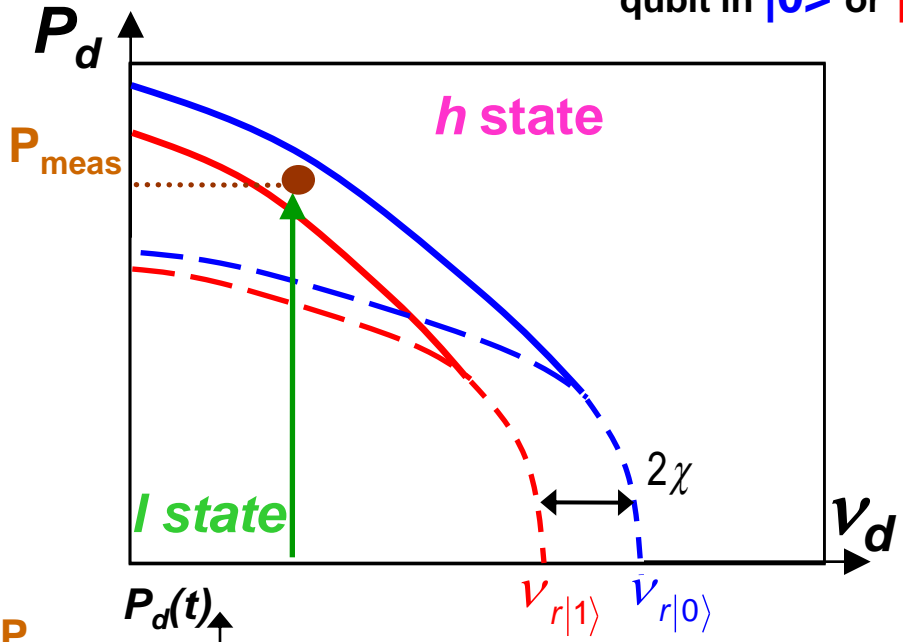


Readout of transmon with CJBA

MW drive : $P_d(t)$, ν_d

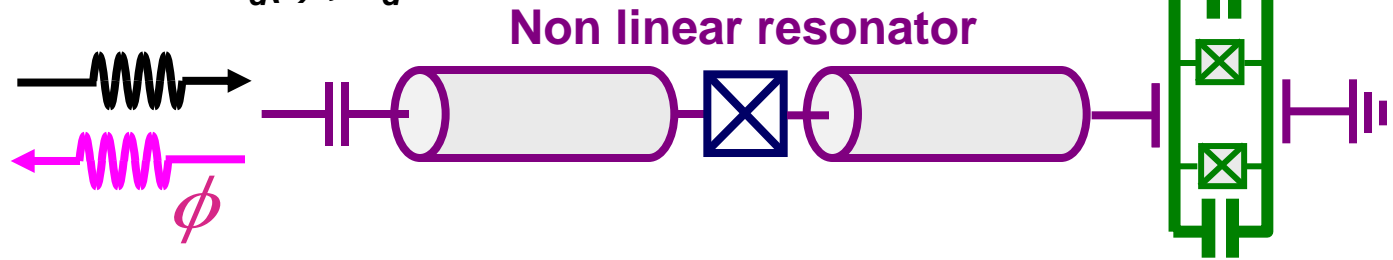


qubit in $|0\rangle$ or $|1\rangle$

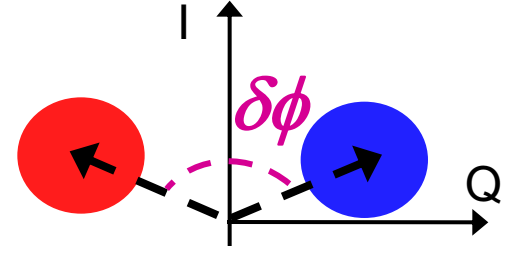
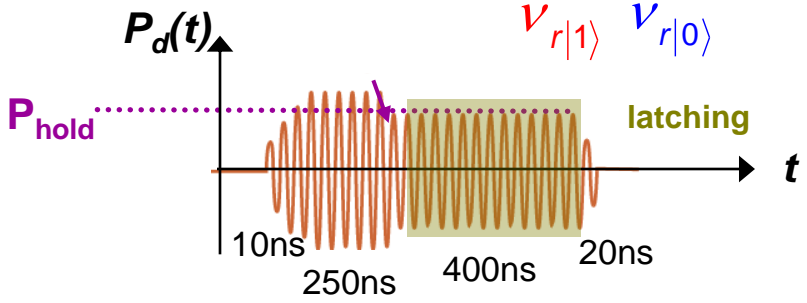
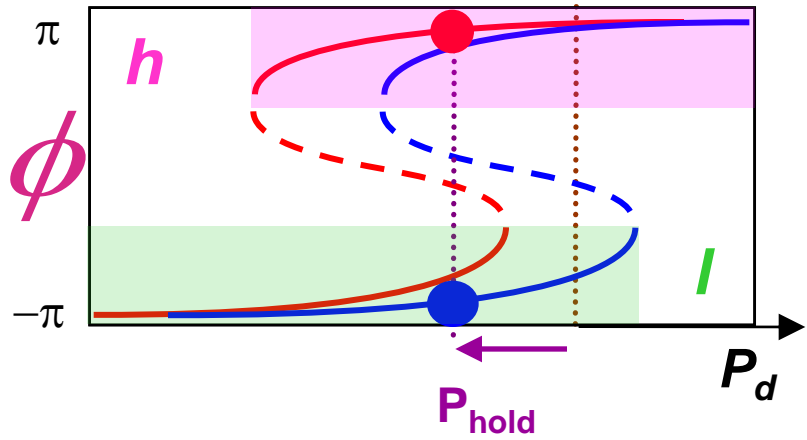
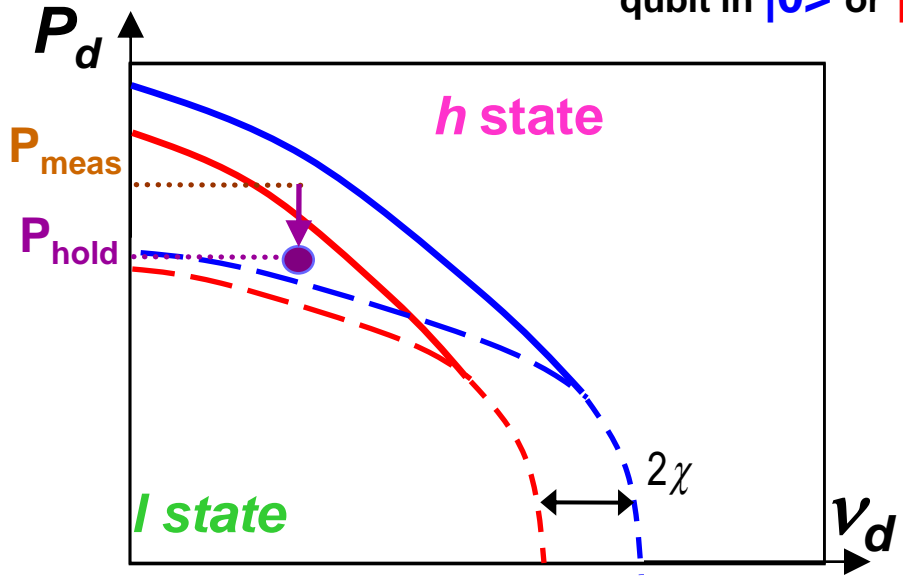


Readout of transmon with CJBA

MW drive : $P_d(t)$, v_d

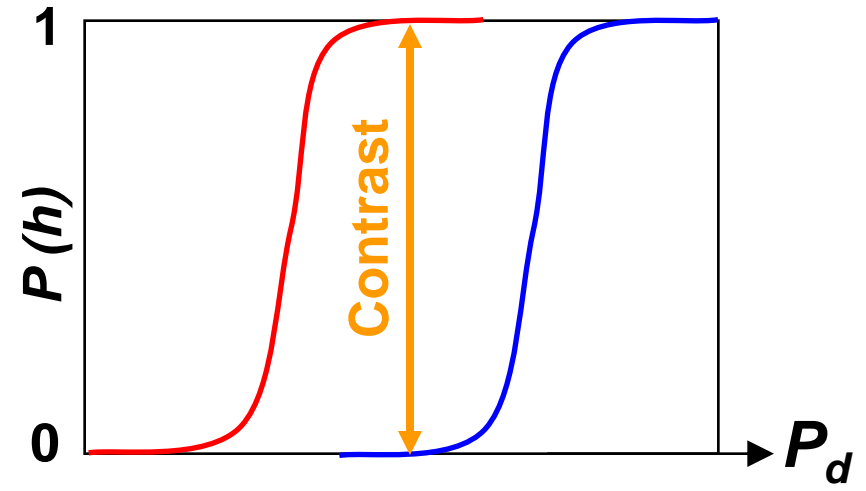
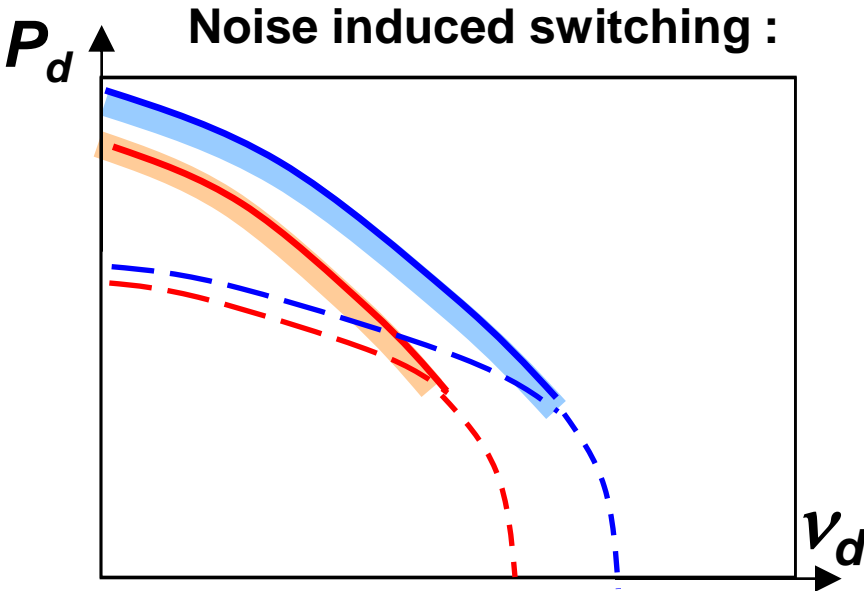
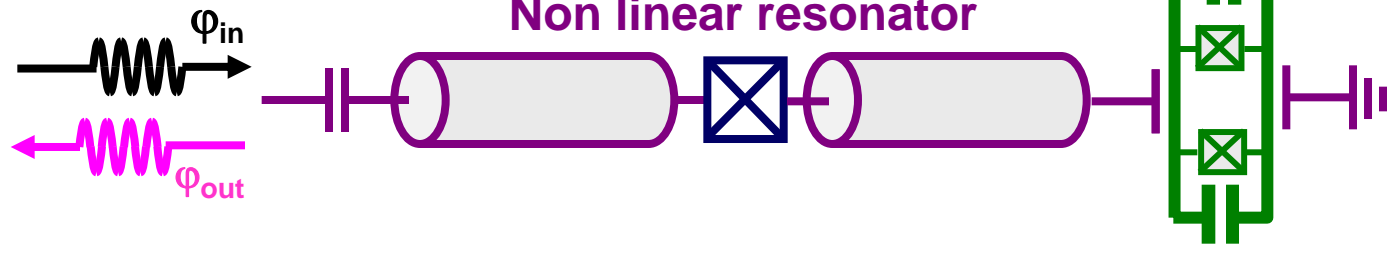


qubit in $|0\rangle$ or $|1\rangle$



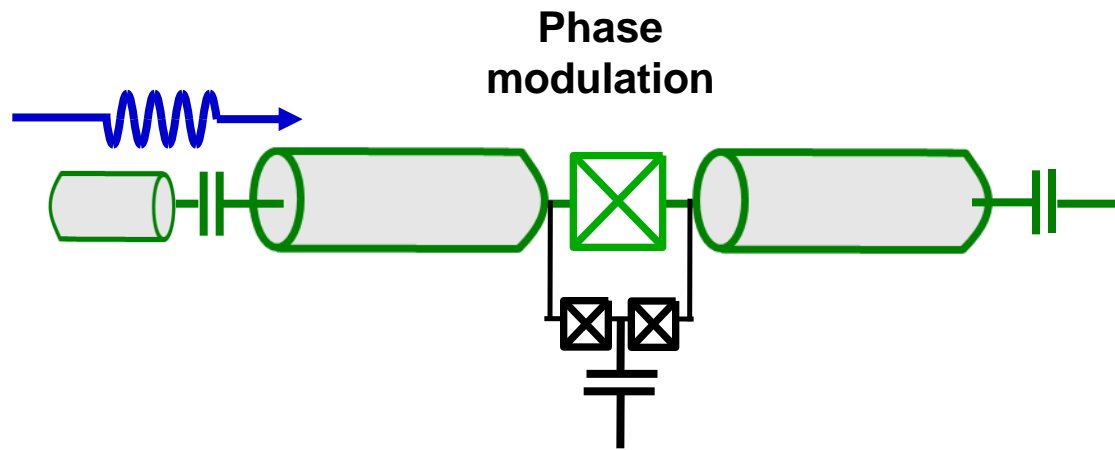
Readout of transmon with CJBA

MW drive : $P_d(t)$, ν_d

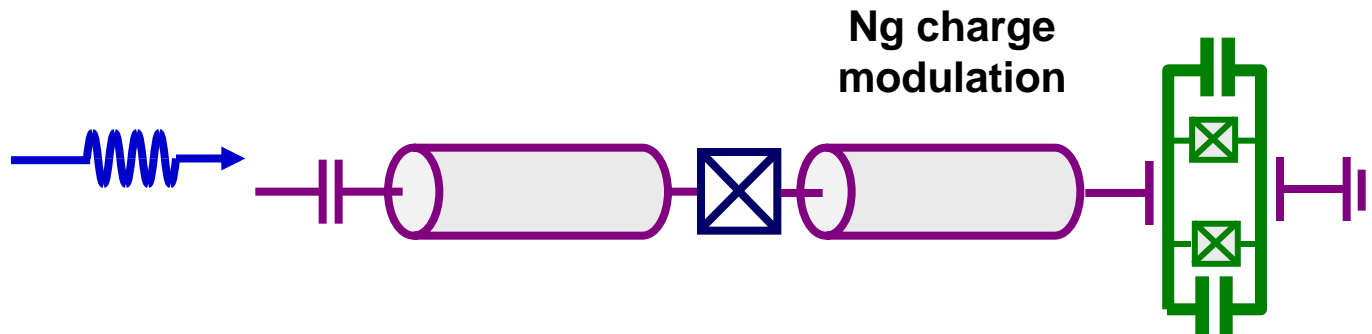


"S-curves" shift > S width → Single shot readout

The bonus of transmon readout with CJBA



Eigenstates swept
// Stark shifted energy
sweeps a wide
frequency range

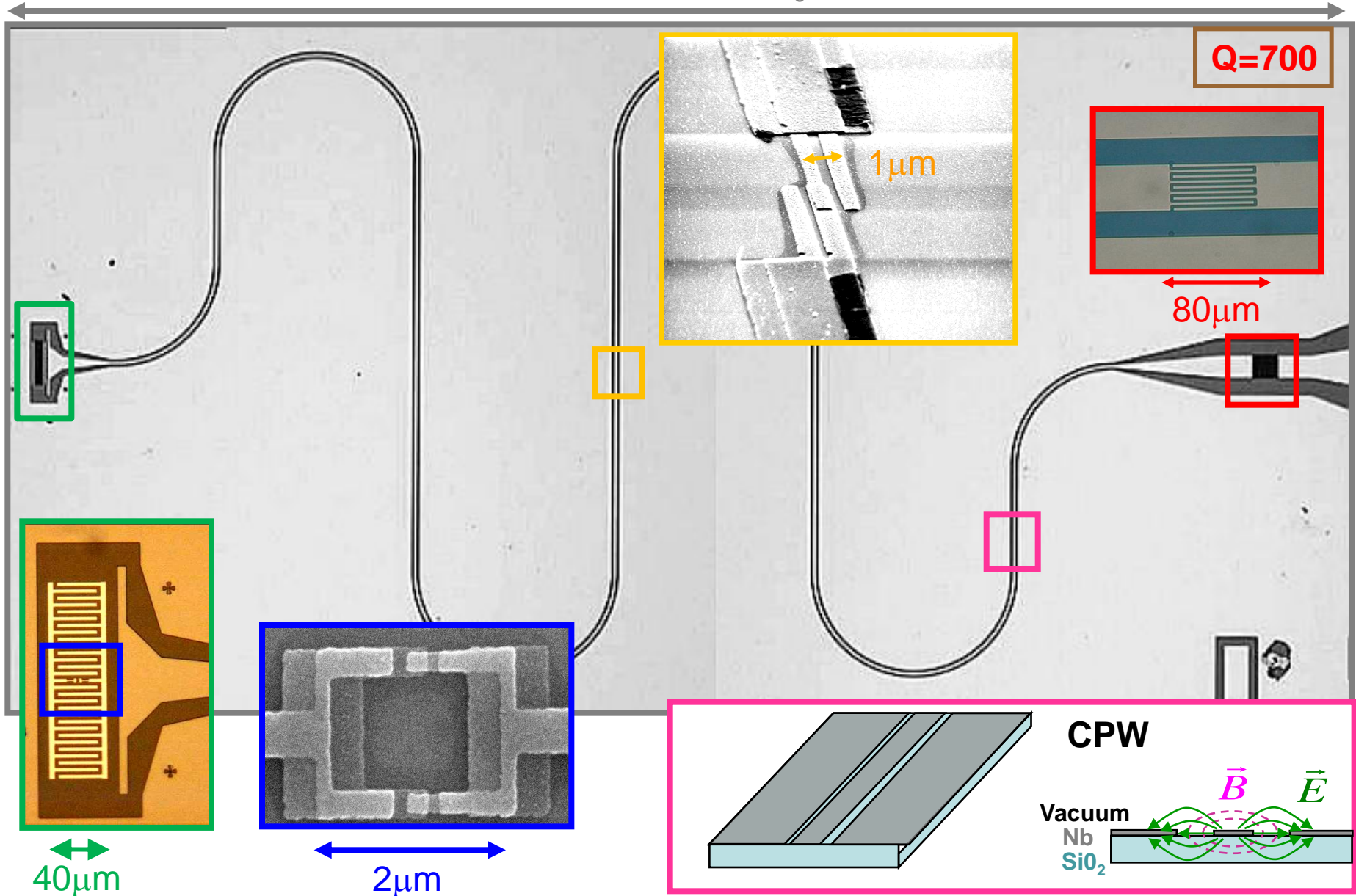


Eigenstates
Insensitive to charge
Changes; small
⊥ Stark shift only

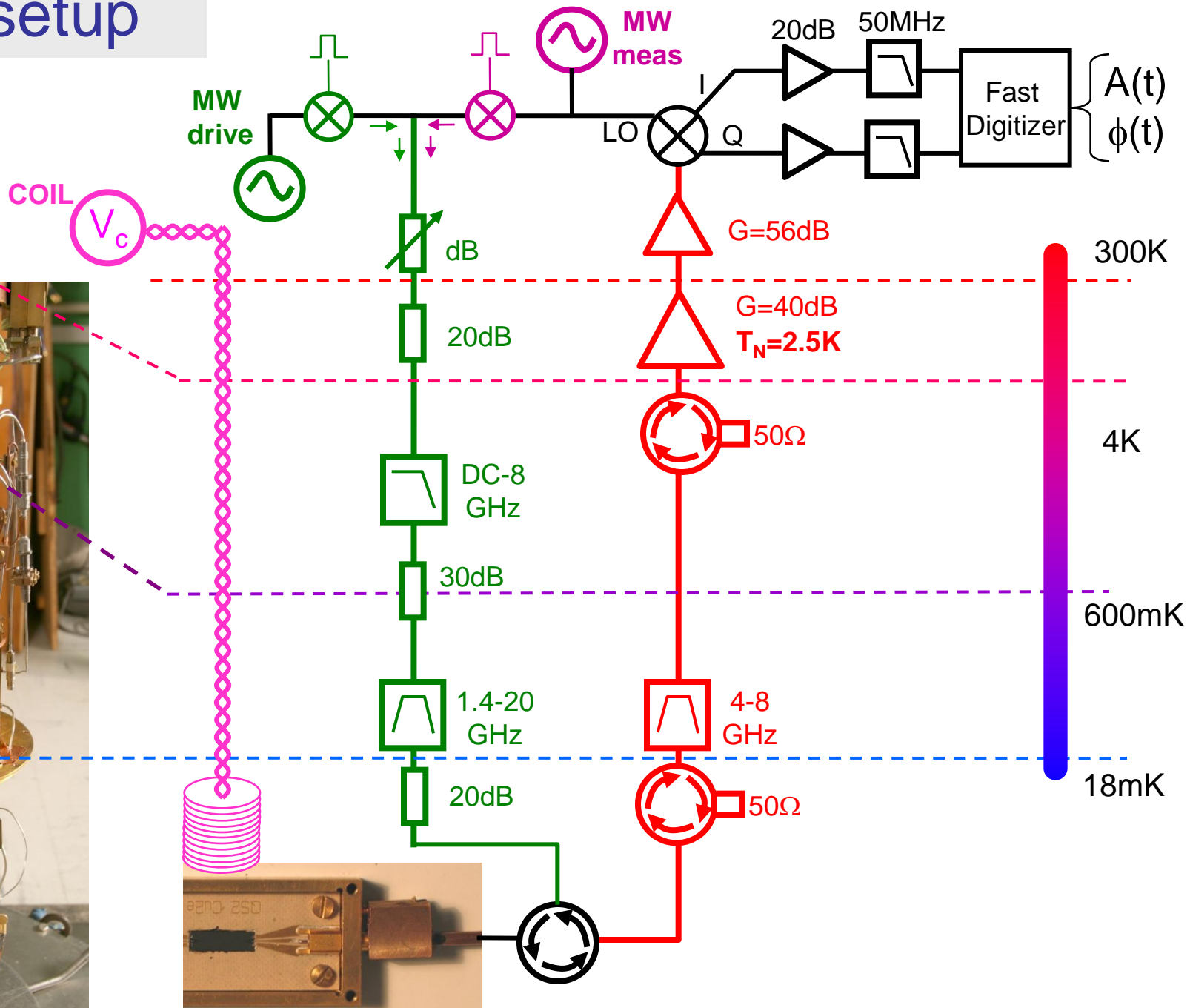
Charge insensitivity combined with bifurcation at low photon number

Physical implementation

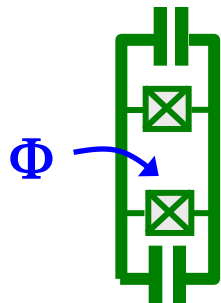
5 mm ($f_0=6.5\text{GHz}$)



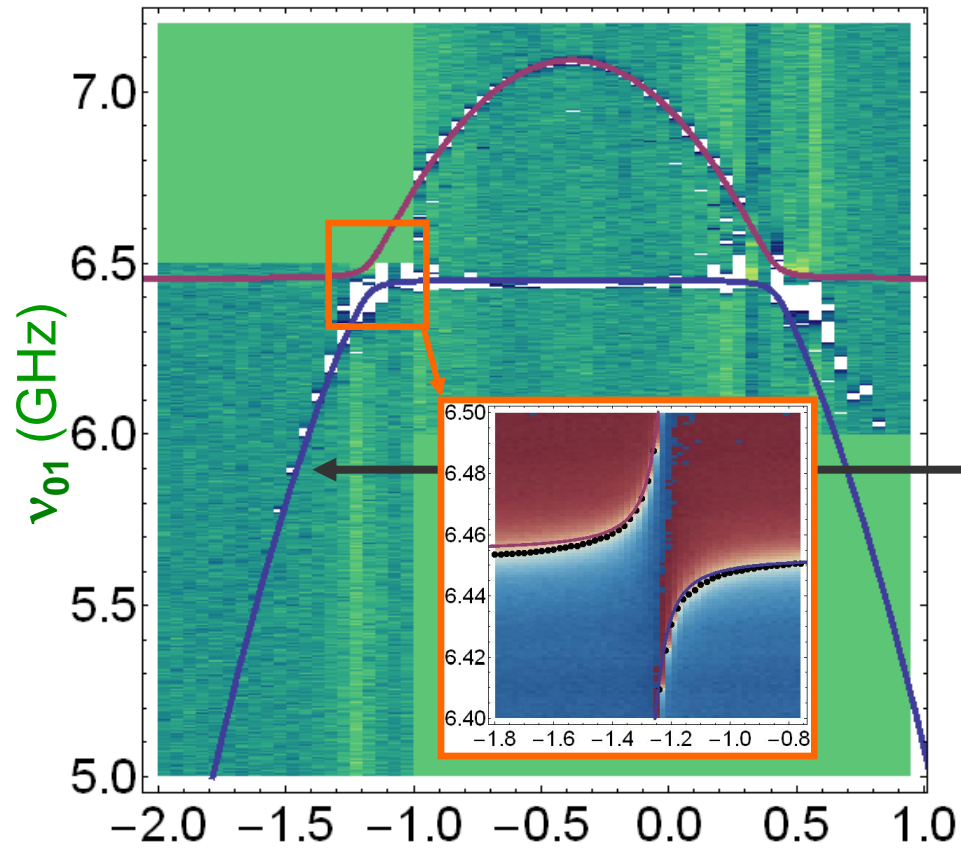
The setup



Qubit and cavity characterization

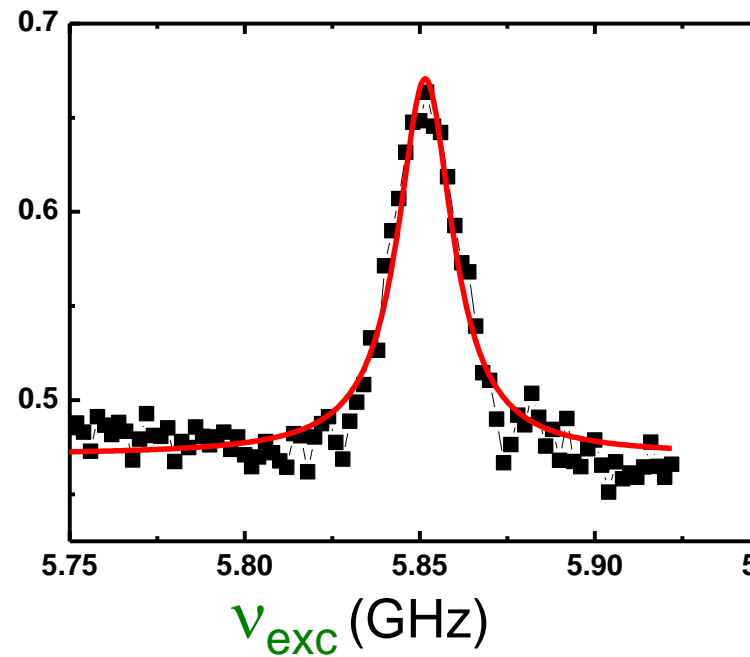


Spectroscopy of the coupled system

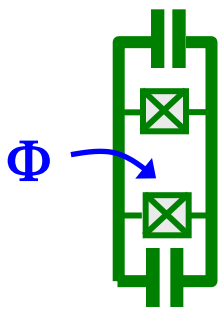


Φ/Φ_0

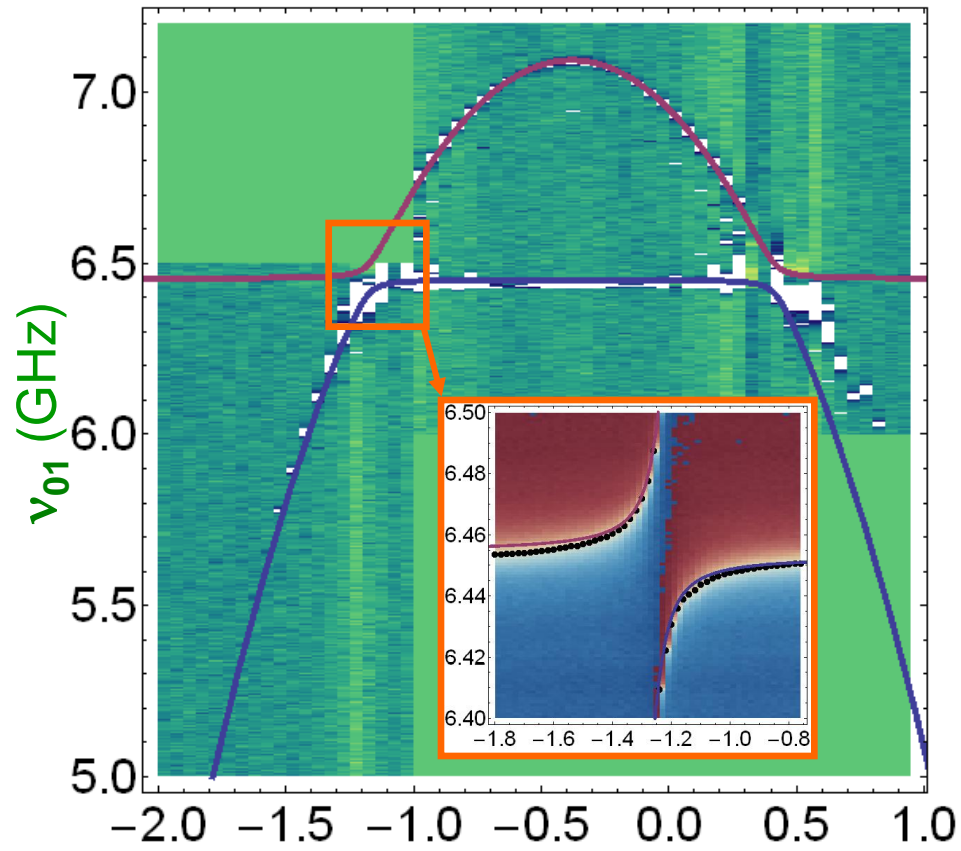
$E_c = 1.2$ GHz
 $E_j = 23$ GHz
 $g = 45$ MHz



Qubit and cavity characterization



Spectroscopy of the coupled system

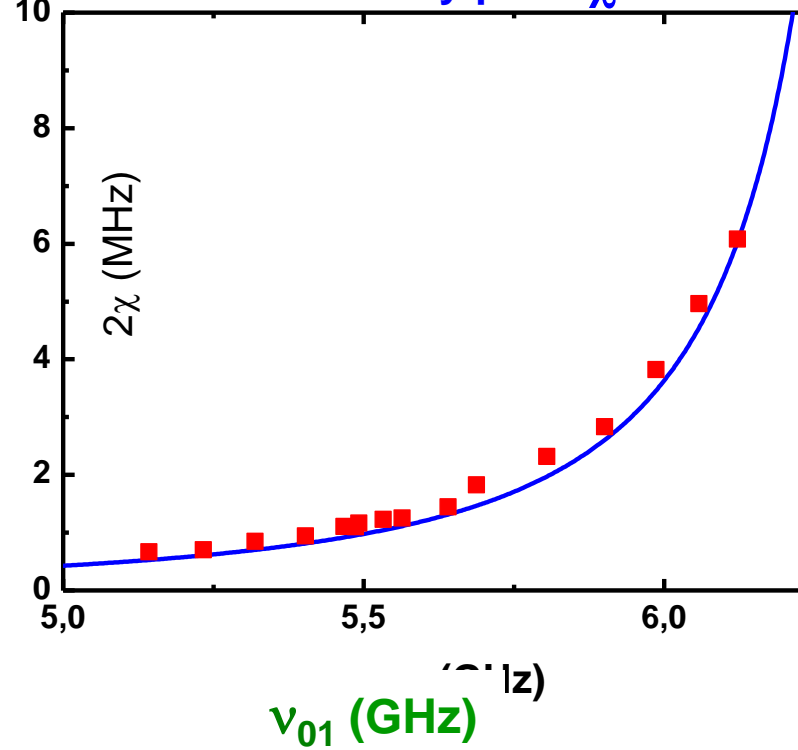


Φ/Φ_0

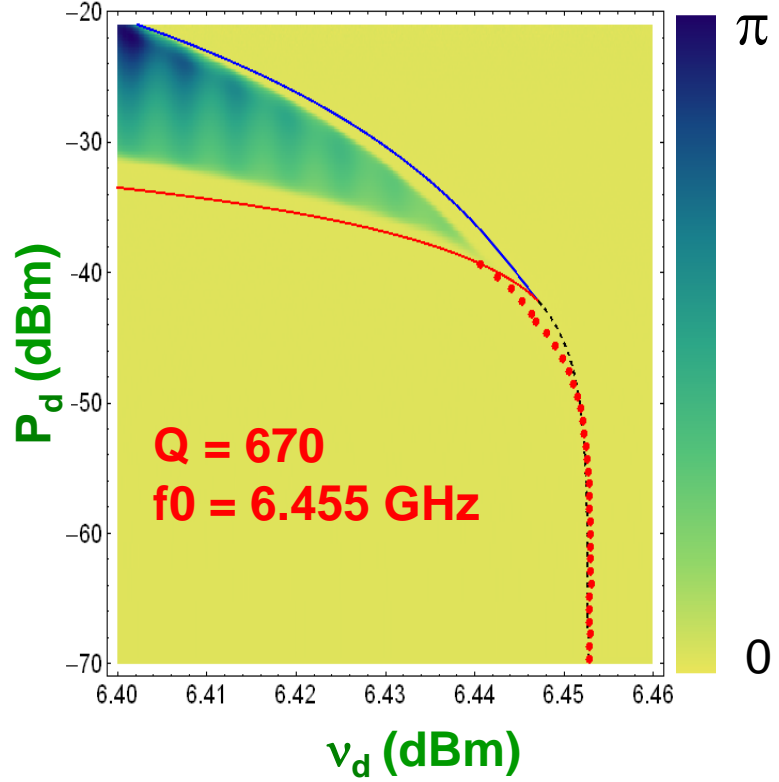
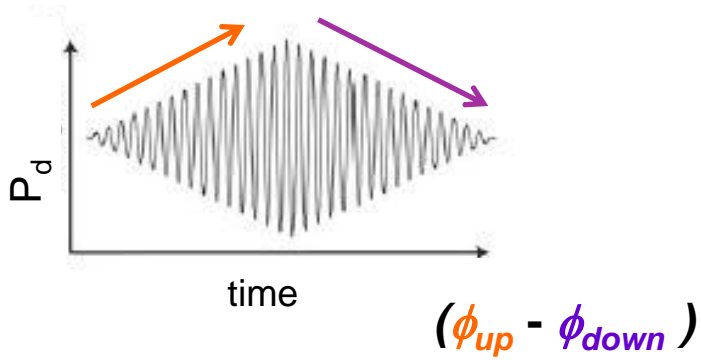
→

$E_c = 1.2 \text{ GHz}$
 $E_j = 23 \text{ GHz}$
 $g = 45 \text{ MHz}$

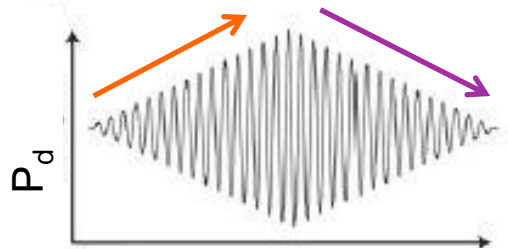
Measure of cavity pull 2χ



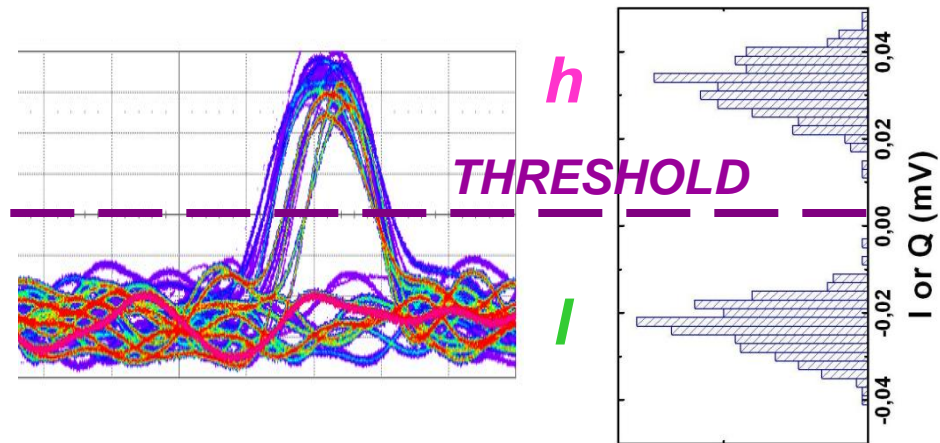
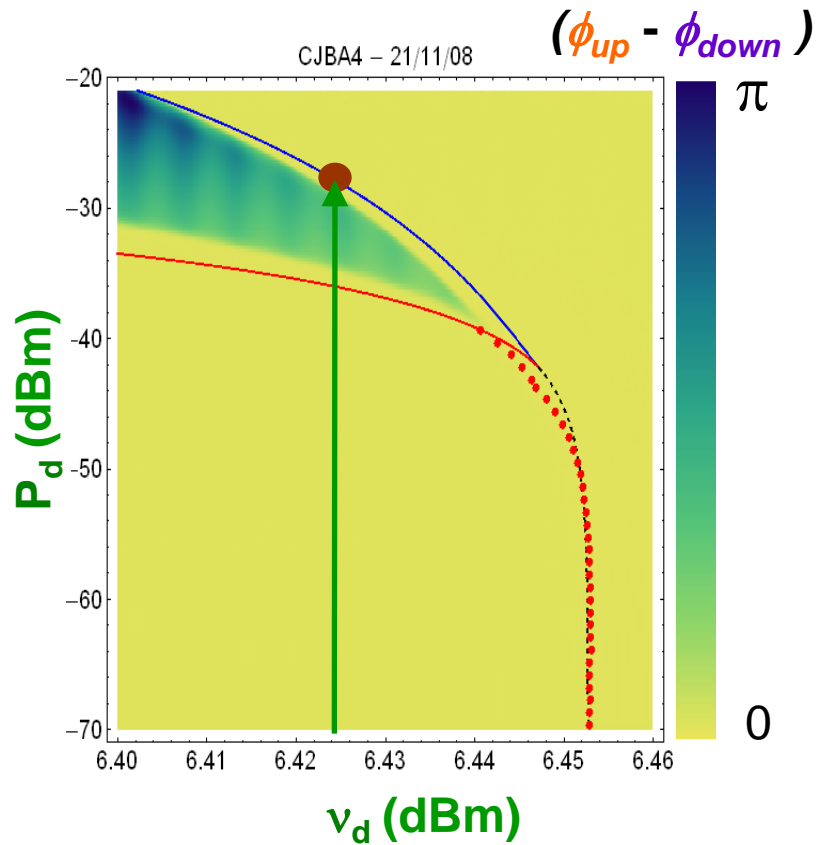
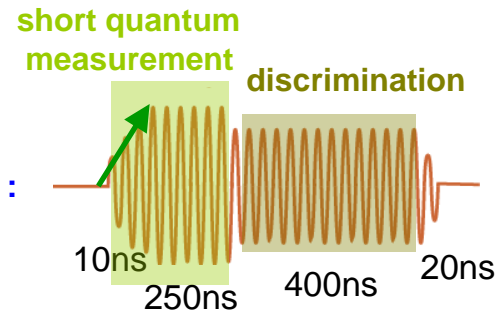
Cavity JBA characterisation



Cavity JBA characterisation

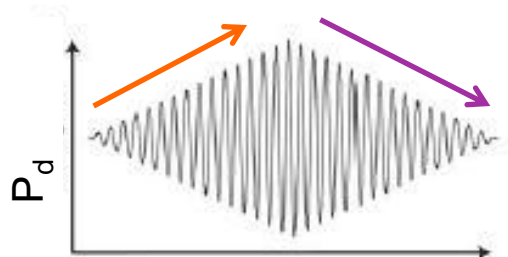


Repetition of the sequence :

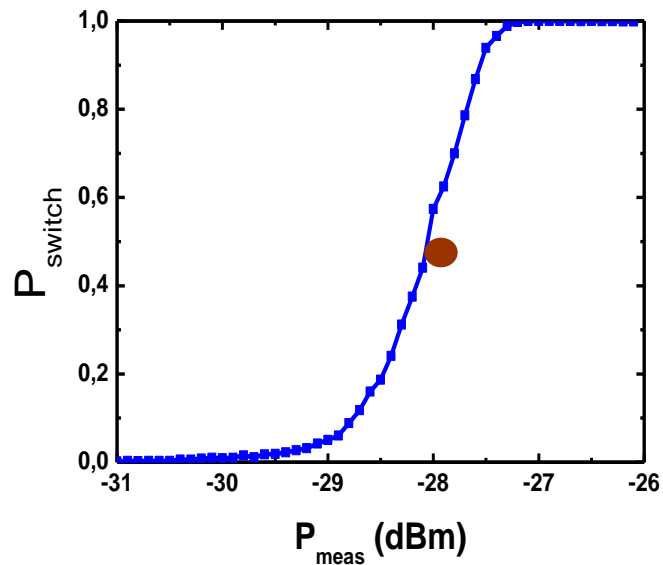
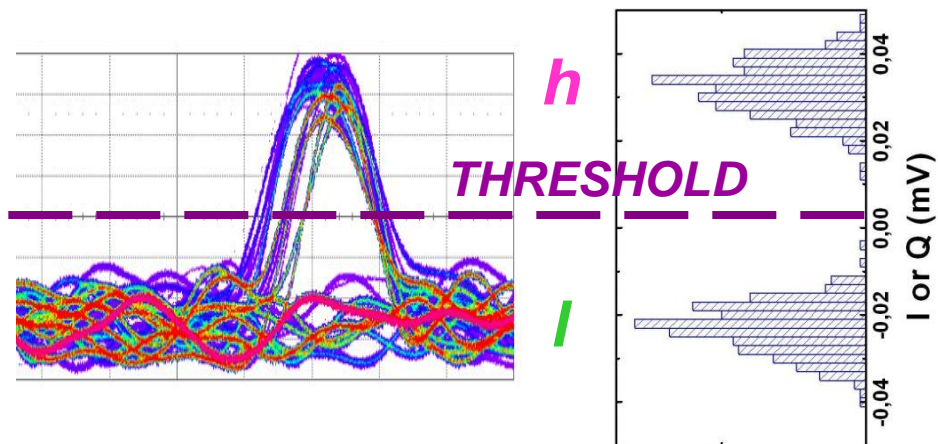
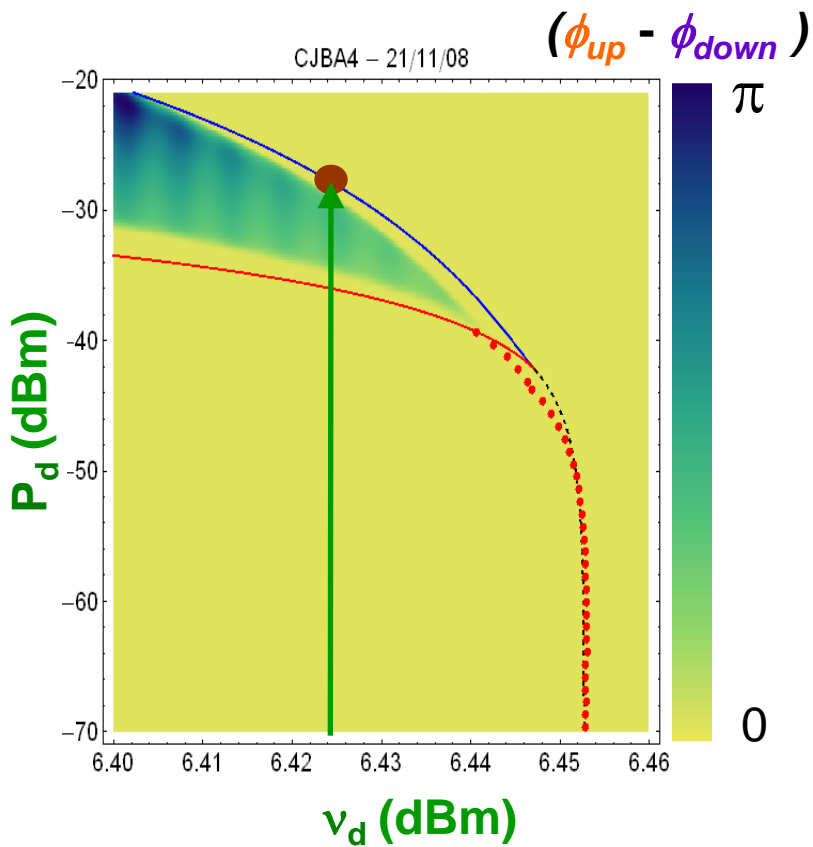
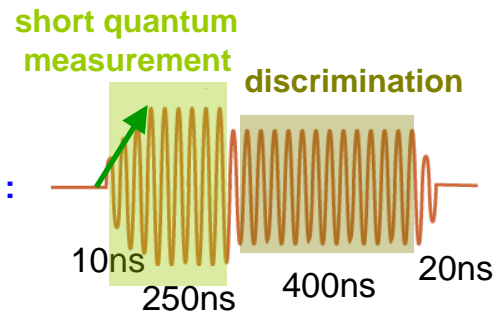


No discrimination errors

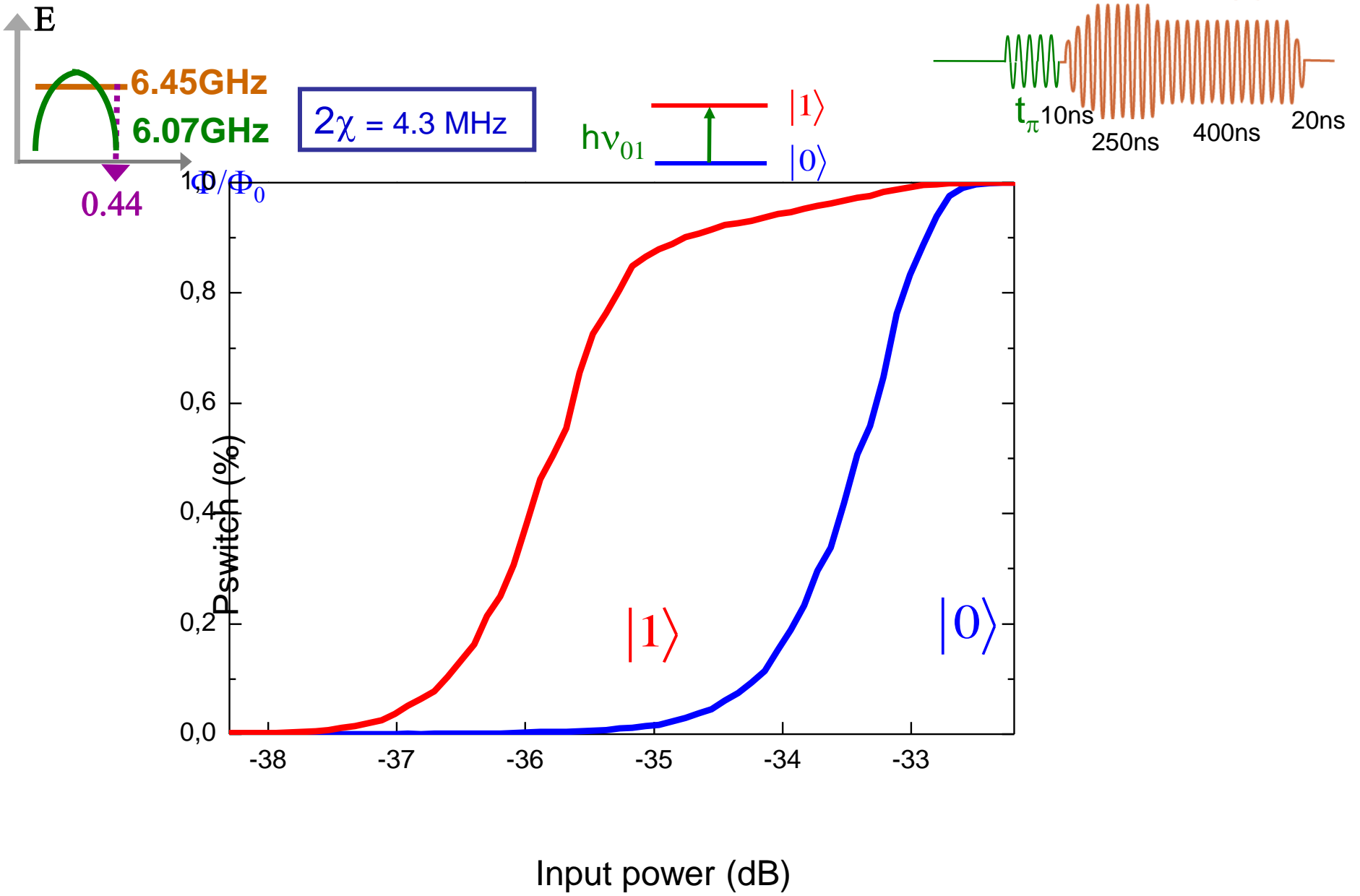
Cavity JBA characterisation



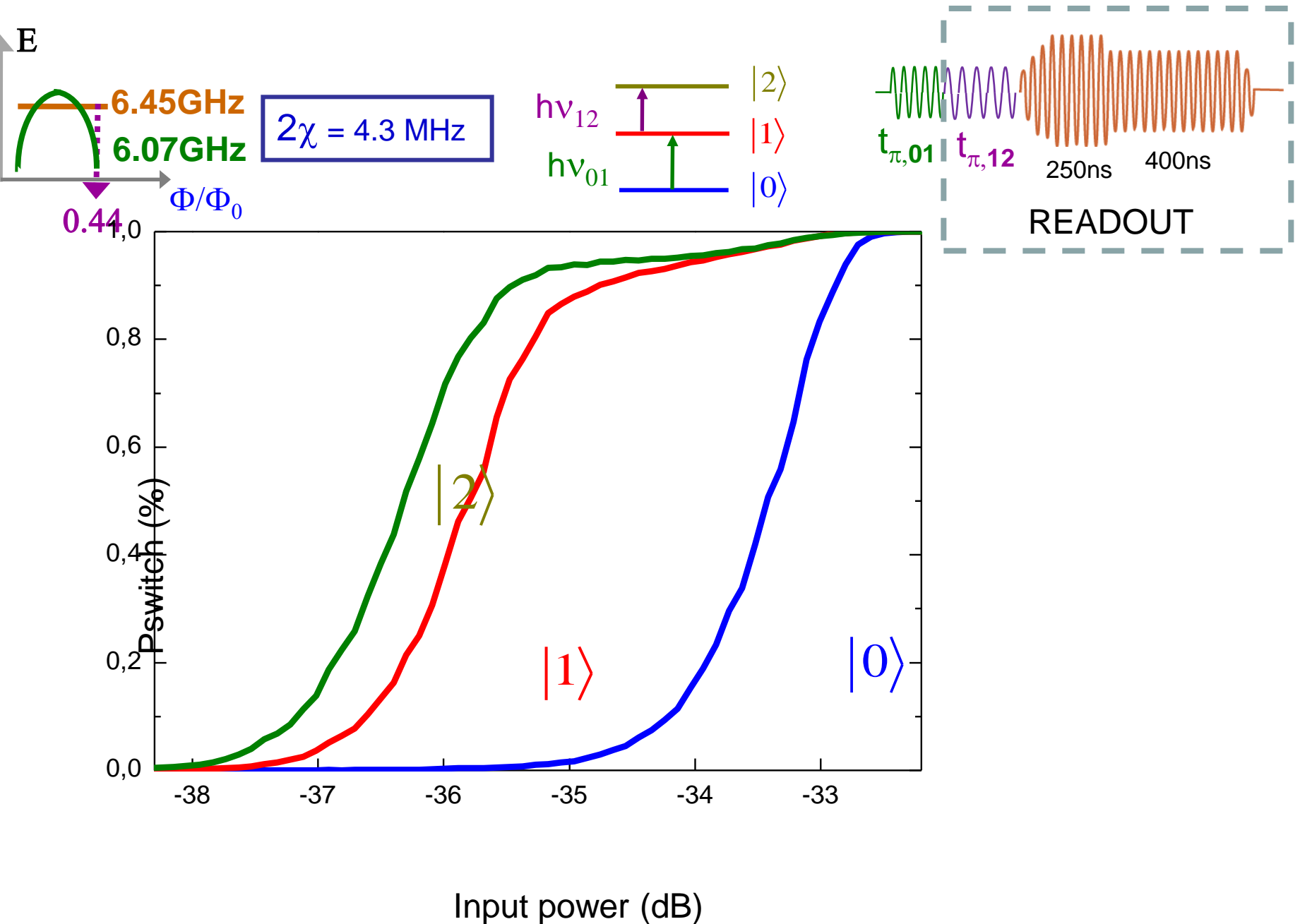
Repetition of the sequence :



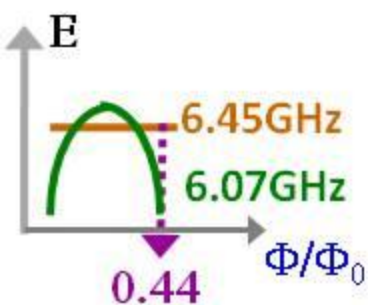
Readout of qubit state 400 MHz below cavity



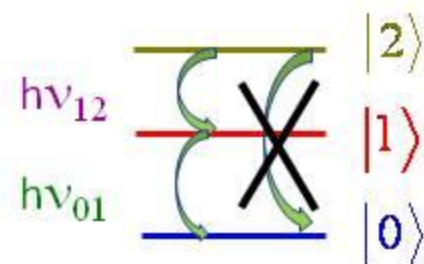
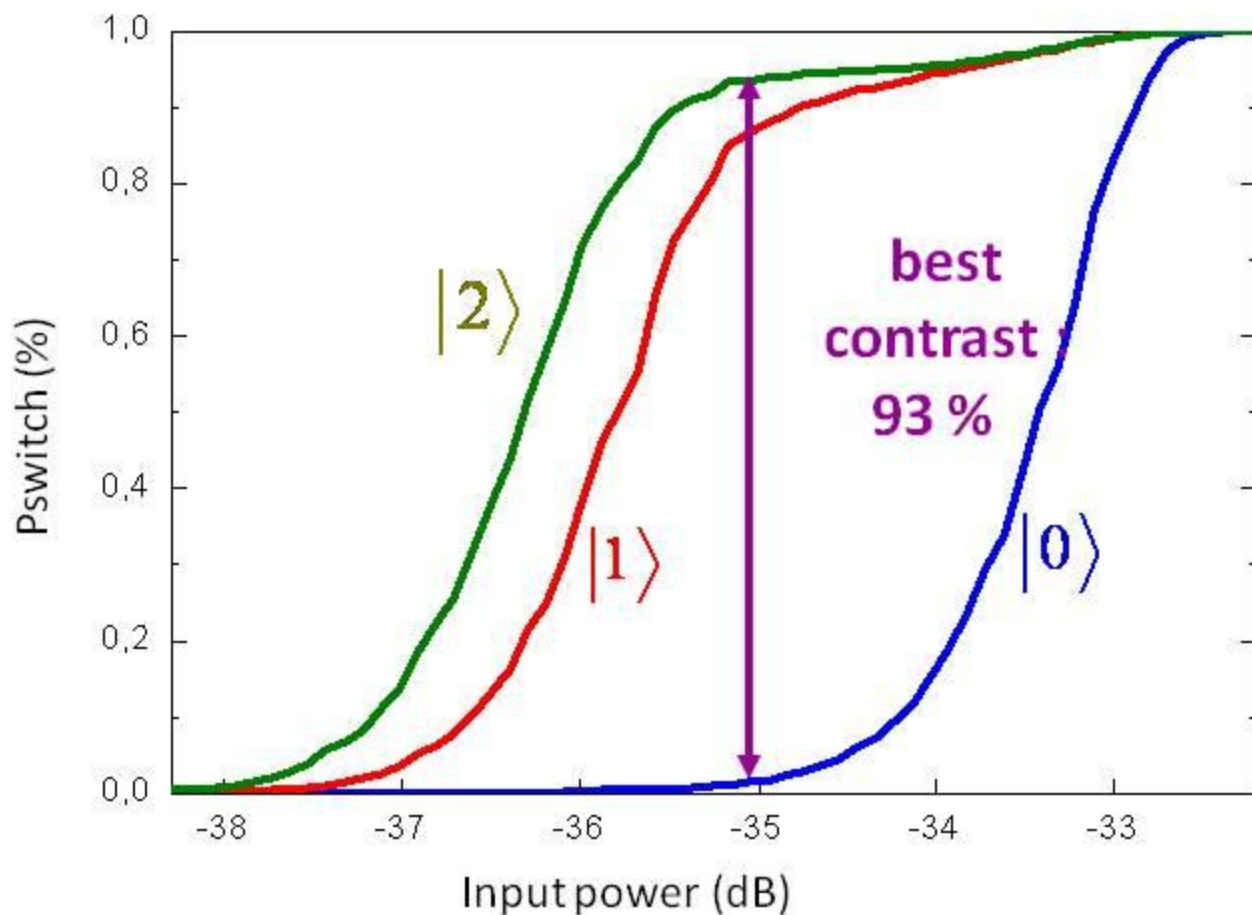
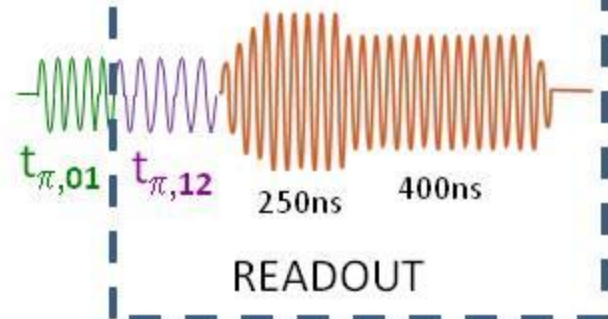
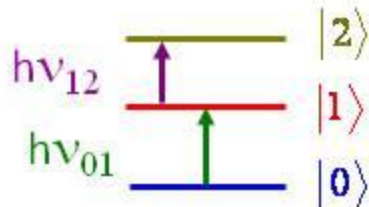
Climbing one extra step yields better fidelity ...



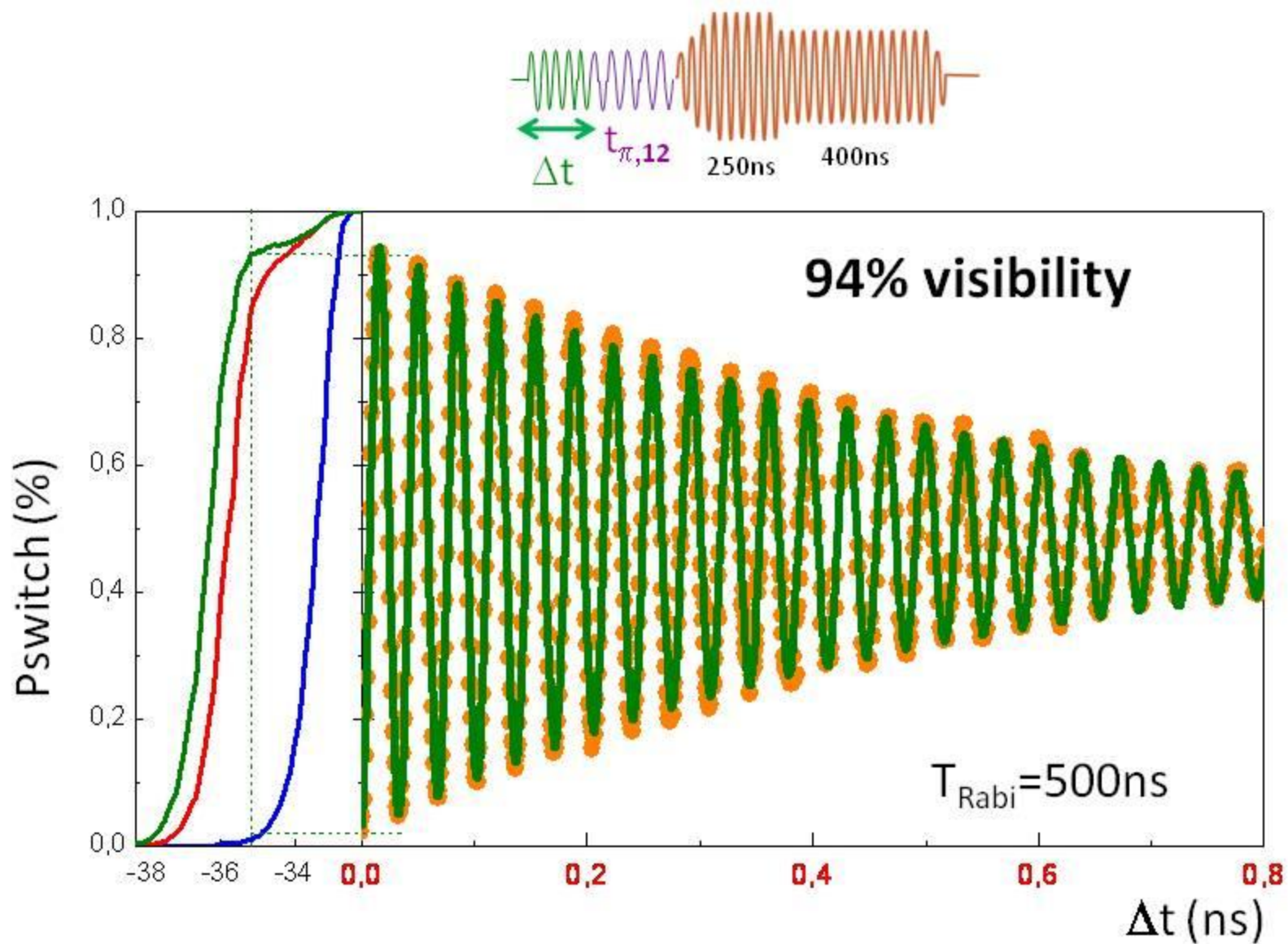
Climbing one extra step yields better fidelity ...



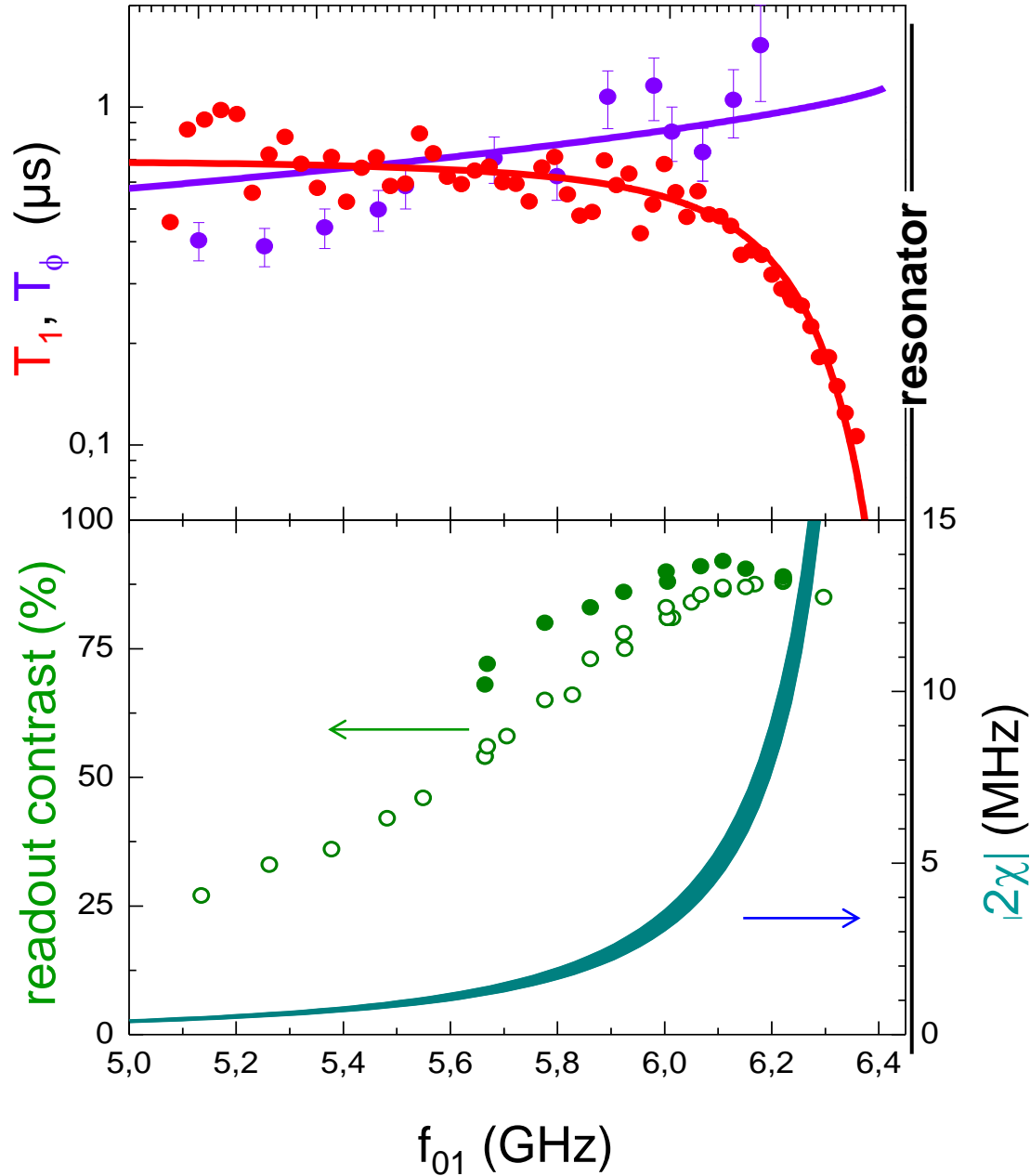
$$2\chi = 4.3 \text{ MHz}$$



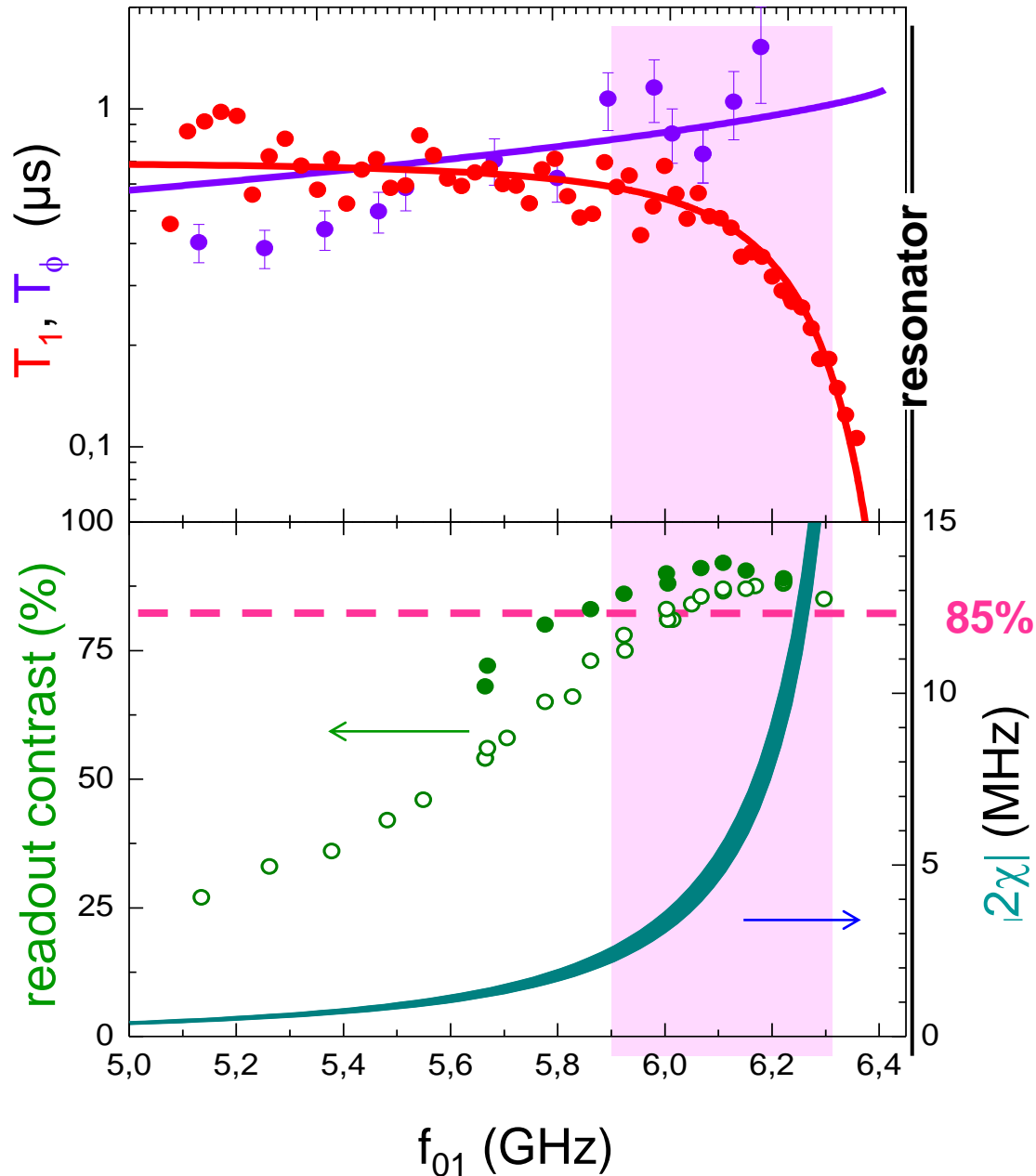
Single-shot high visibility Rabi oscillations



Trade-off readout contrast – coherence ?



readout fidelity compatible with coherence



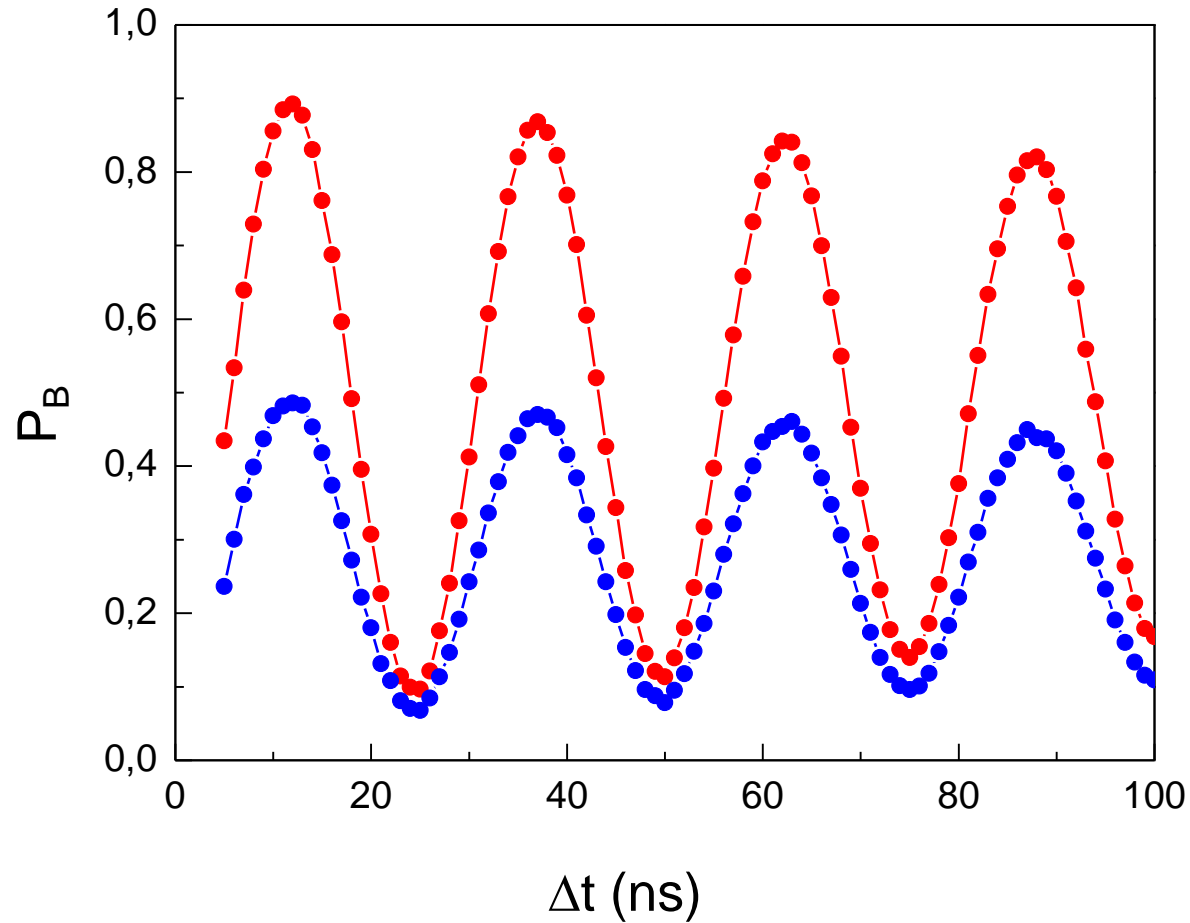
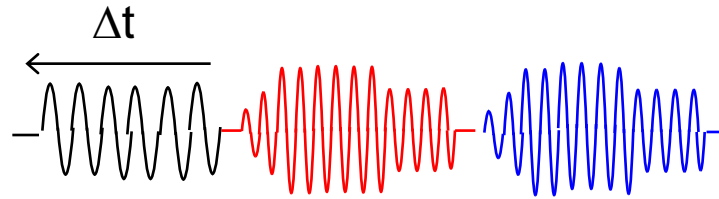
Projection fidelity ?

Projective measurement of $|\Psi\rangle = \alpha|0_1\rangle \otimes |\Psi_{2\dots N}\rangle + \beta|1_1\rangle \otimes |\Psi'_{2\dots N}\rangle$

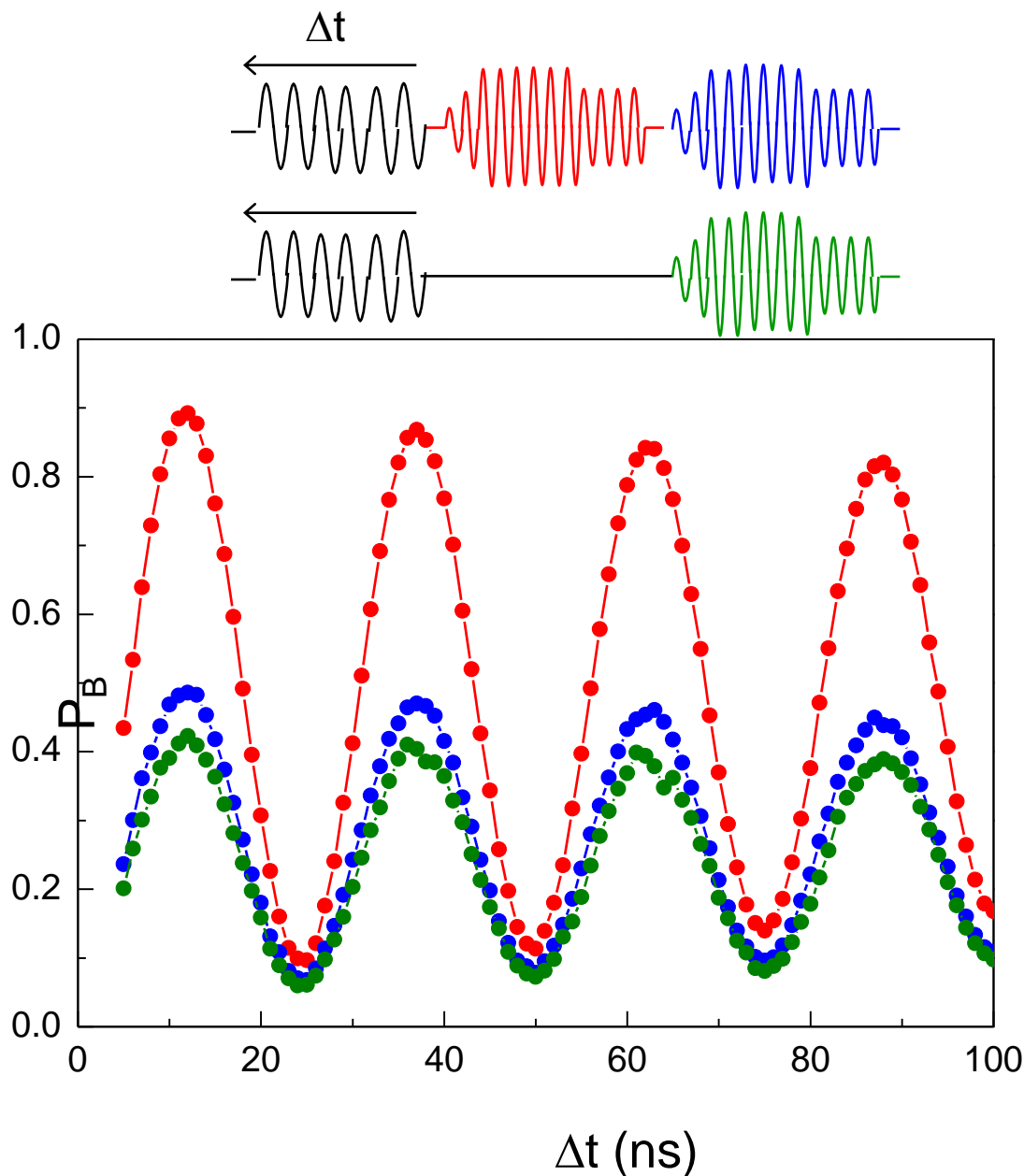
yields $\left\{ \begin{array}{l} \text{readout 0 and state } |0_1\rangle \otimes |\Psi_{2\dots N}\rangle \quad \text{with prob } |\alpha|^2 \\ \text{or} \\ \text{readout 1 and state } |1_1\rangle \otimes |\Psi'_{2\dots N}\rangle \quad \text{with prob } |\beta|^2 \end{array} \right.$

**QND character can be tested
with repeated measurements**

relaxation limited test of projection fidelity



relaxation limited test of projection fidelity



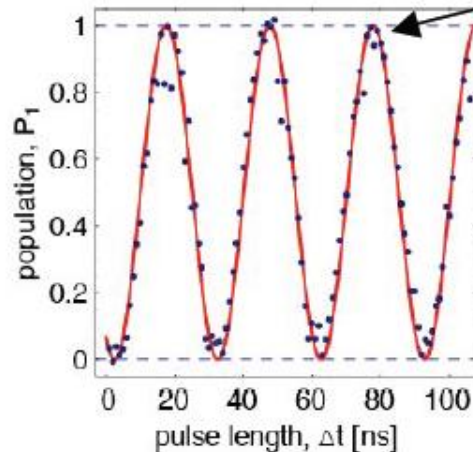
**No EXTRA
Relaxation
during
readout**

**Data compatible
with non-demolition**

Claims above 90% : a brief (critical) review

High visibility Rabi oscillations (Yale, Wallraff et al. ,PRL 2005)

Rabi oscillations:



visibility $95 \pm 5\%$

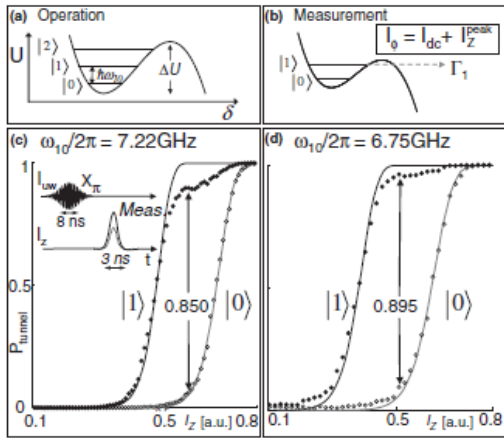
for superconducting qubits:

- high visibility

we have observed high visibility in the oscillations of state population of a superconducting qubit. The tem-

**~95% population inversion,
but no high fidelity readout**

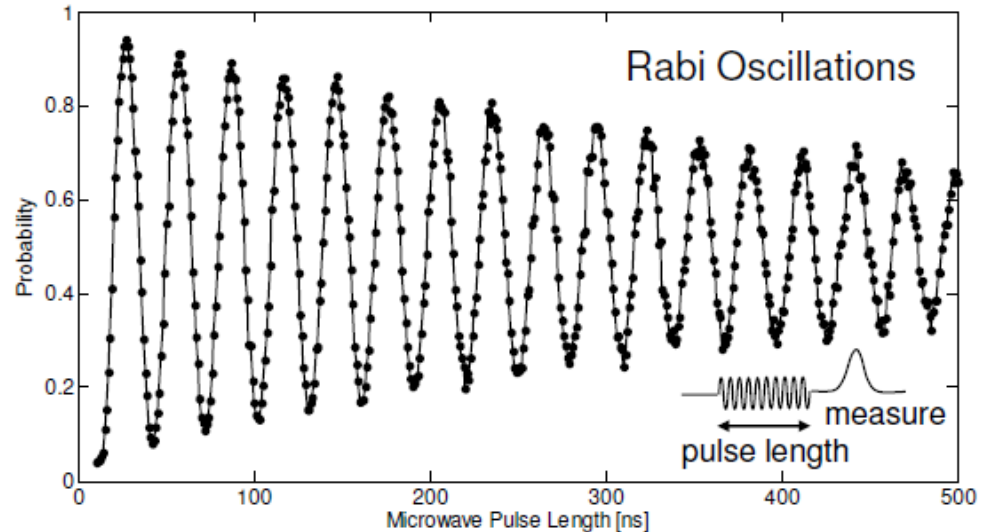
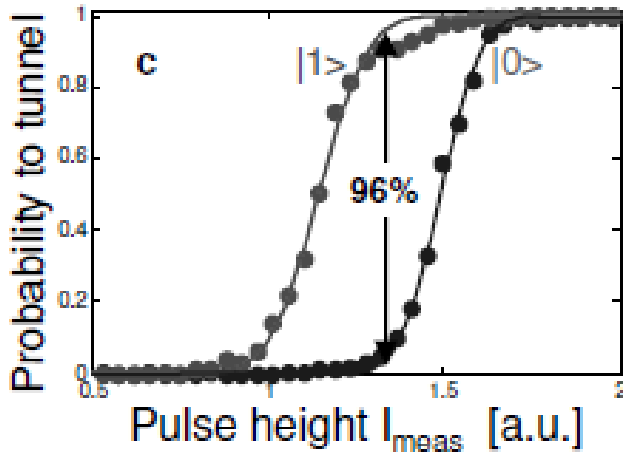
High measurement fidelity (J. Martinis, UCSB)



Lucero et al., PRL 100 (2008)

~90% readout contrast
(destructive)

J. Martinis' review, QIP 8(2009)

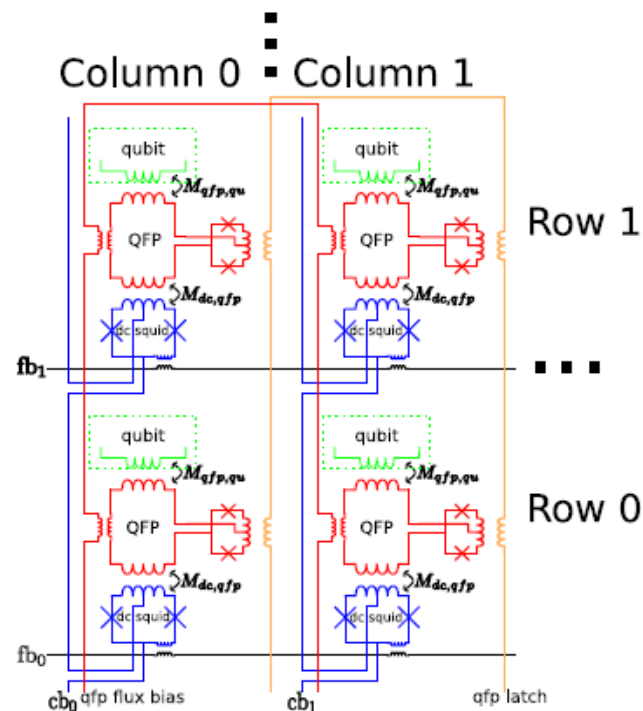


The Rabi oscillations have fidelity of about 90%, a value reasonably close to the theoretical expectation 96% [15]. The energy decay time for this qubit is $T_1 = 600$ ns.

Rabi oscillations with about 90% fidelity

A record 99.9999% claim from DWAVE

Berkley et al.,
arXiv 0905.0891



QFP (Quantum Flux Parametron):
tunable barrier device

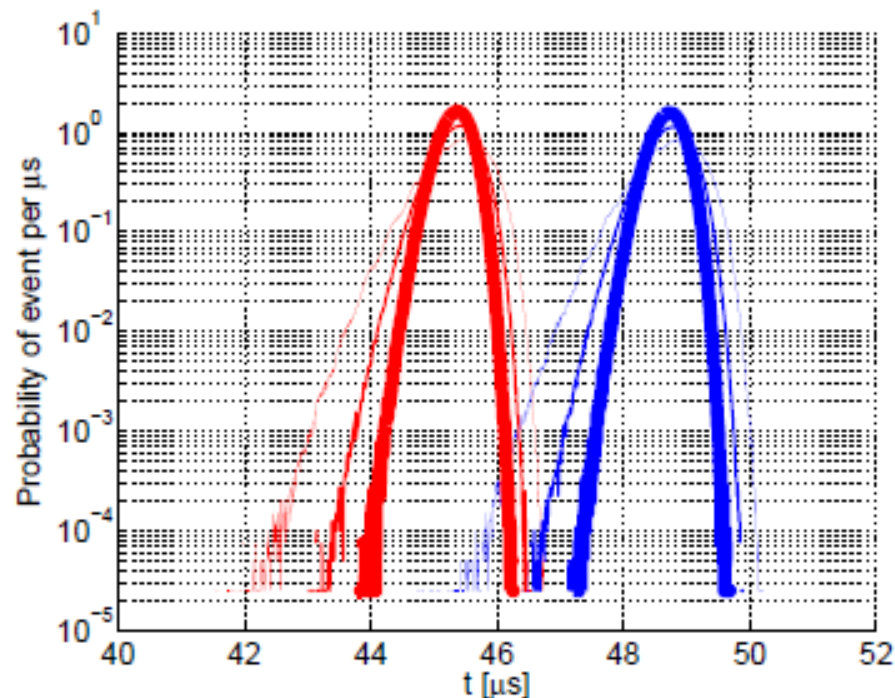


Fig. 6: Improving readout fidelity with repeated dc SQUID sampling of the QFP state. The dc SQUID has a current ramp applied which lasts approximately $50 \mu\text{s}$. The red and blue curves correspond to different initialized flux states of the qubit (which is then adiabatically transferred to the QFP). There are three separate traces showing the probability per time of the dc SQUID switching as the current bias is ramped. The three lines going from thin to thick correspond to 1, 2, and 4 averaged reads of the dc SQUID. Once 4 reads are performed we see no errors in the data set, which was 4 million points. The thick lines on this plot are the fidelity data from which we extract the 99.9999% fidelity quoted in the text.

Not even wrong, but readout fidelity is more than frozen flux state discrimination

Perspectives??

Optimize parameters :

readout fidelity

and

coherence

and

projection fidelity

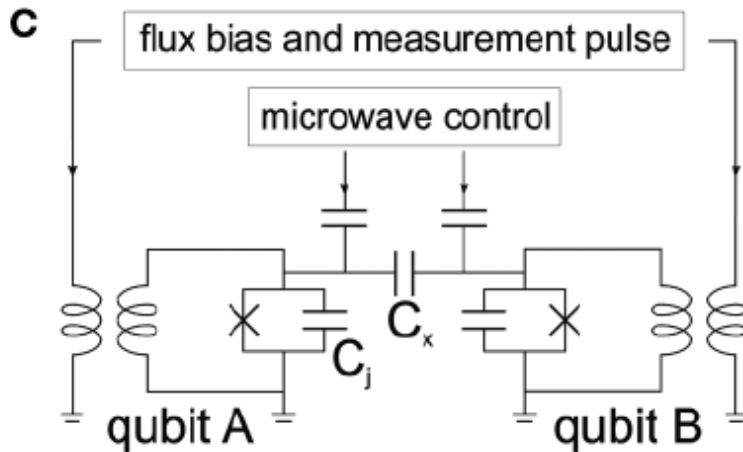
and

in multiqubit circuits

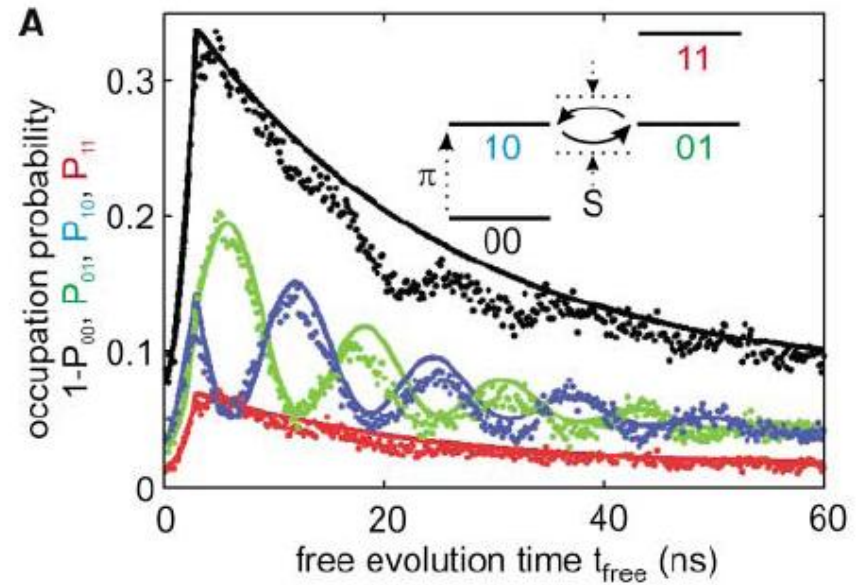
Readout: multiqubit circuits

2 coupled phase qubits

Swapping demonstrated

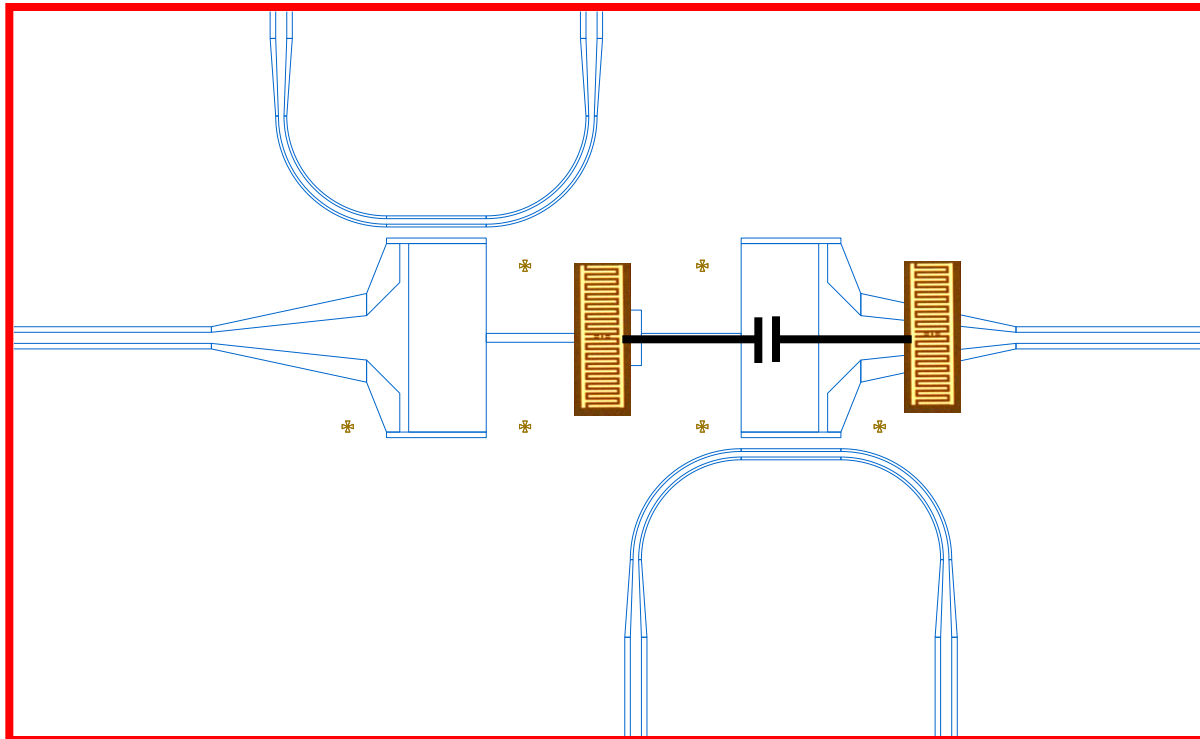
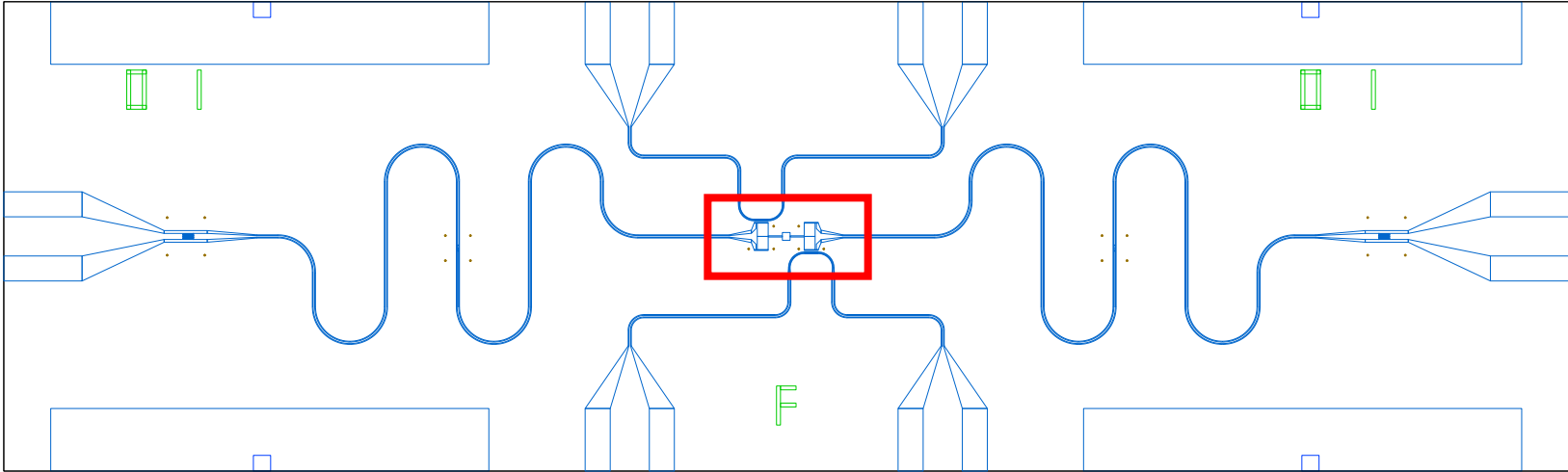


McDermott et al., Science 307 (2005)



~simultaneous & destructive readout: fidelity ~70%

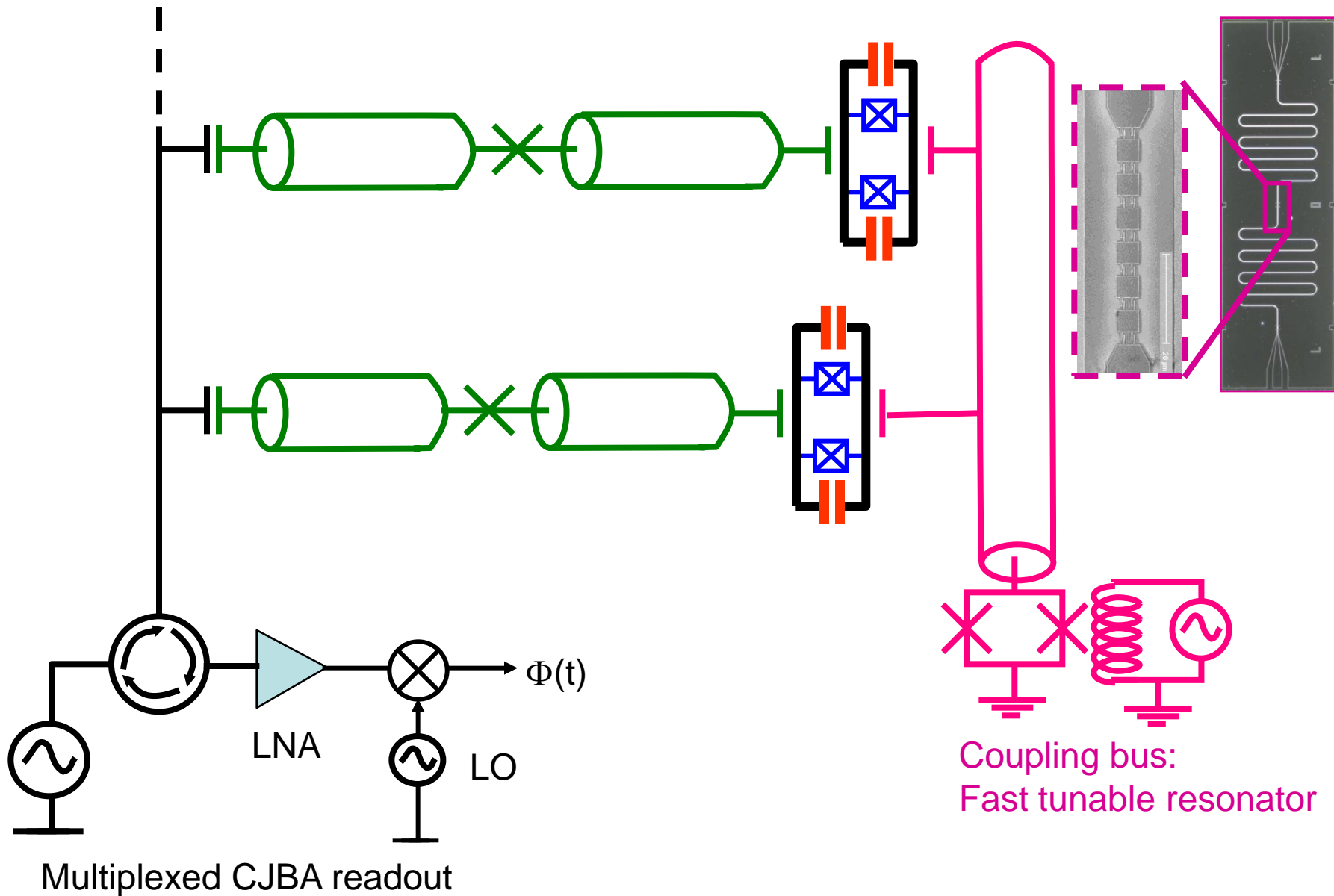
Entangling 2 transmons with individual readouts



for Bell test

Note: just achieved
for phase qubits
(UCSB)

Towards a scalable architecture



QUANTUM ELECTRONICS GROUP

SPEC CEA-Saclay

« Qubit team » :

A. Palacios-Laloy

F. Nguyen

F. Mallet

F. Ong

P. Bertet

D. Vion

D. Esteve

P. Senat

P. Orfila

with the help
of Quantronics
(worldwide)



Qulab
Yale



Quantum mechanical
electronics group,
ENS, CdF



COLLÈGE
DE FRANCE
—1530—

Your questions

